

Regional Training Workshop
Advanced Image Processing of SPECT Studies
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SPECT reconstruction

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Tomography is performed in 2 steps:

1st step = data acquisition (record of projections)

The result is a set of angular projections.

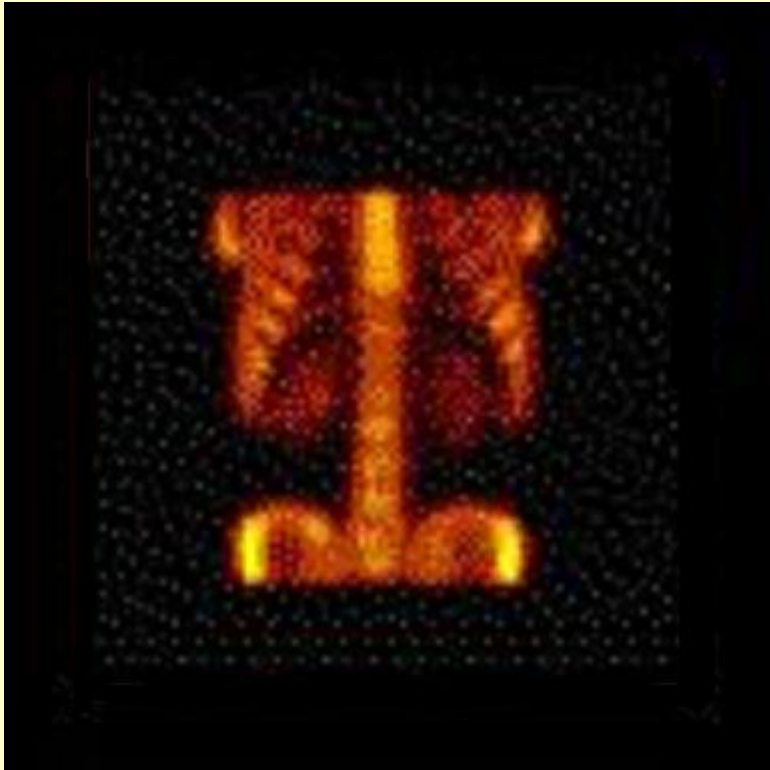
The set of projections of a single slice is called ***sinogram***.

2nd step = image reconstruction from projections

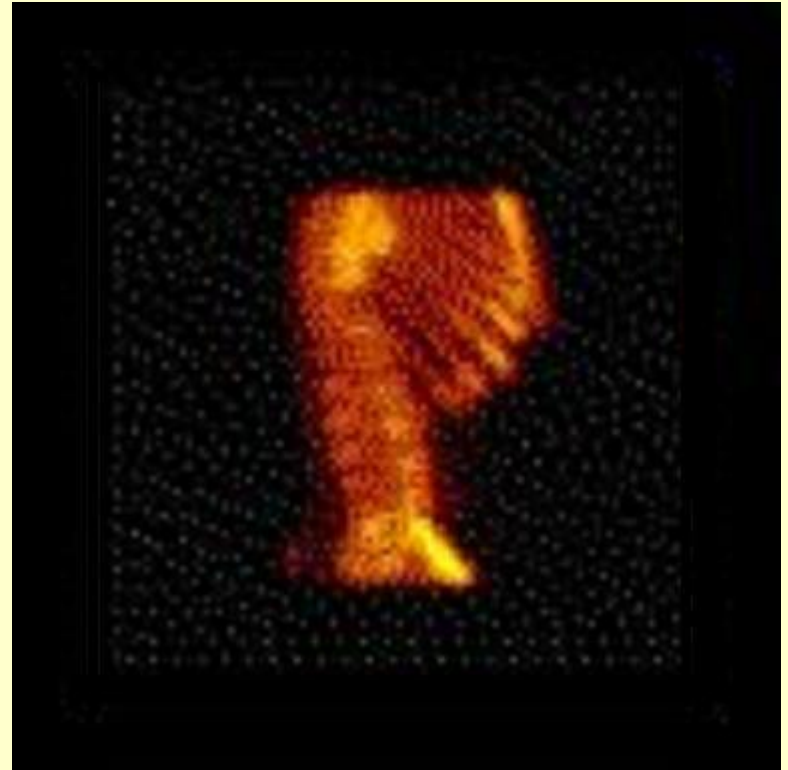
There are 2 groups of reconstruction methods:

analytic (e.g. FBP = filtered back projection) and

iterative (e.g. ART = algebraic reconstruction techniques).



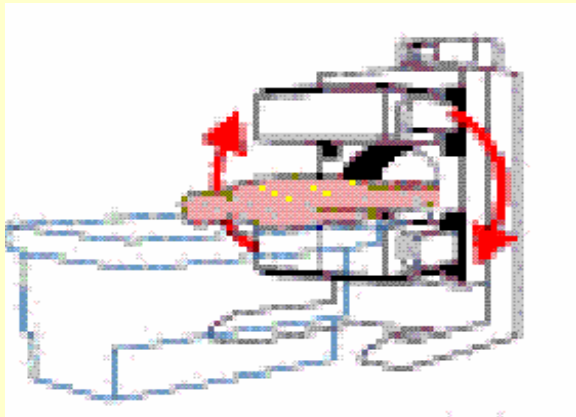
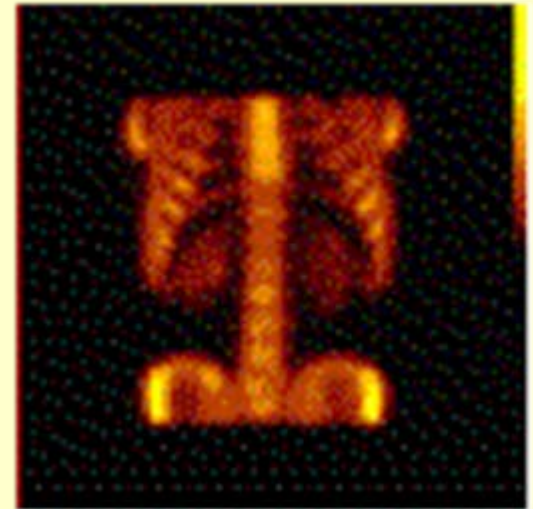
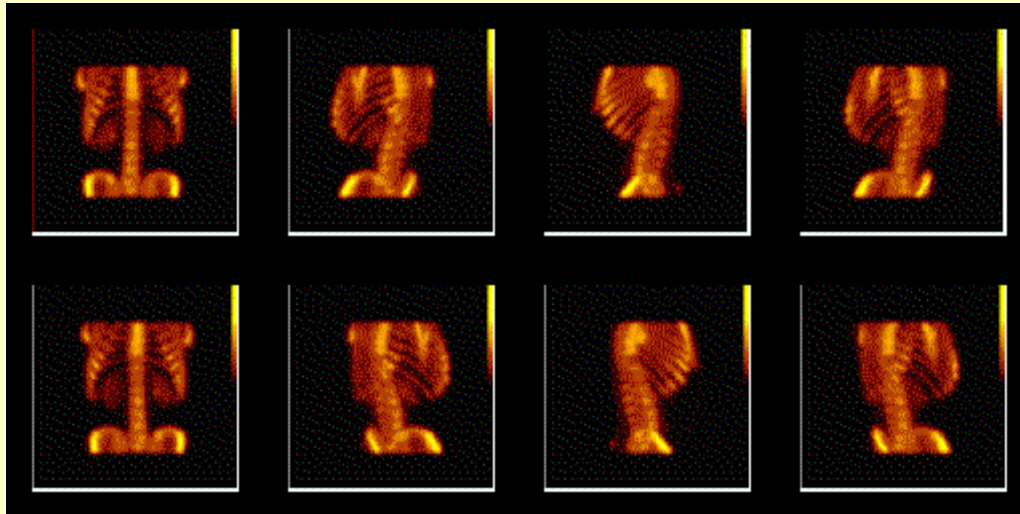
anterior view



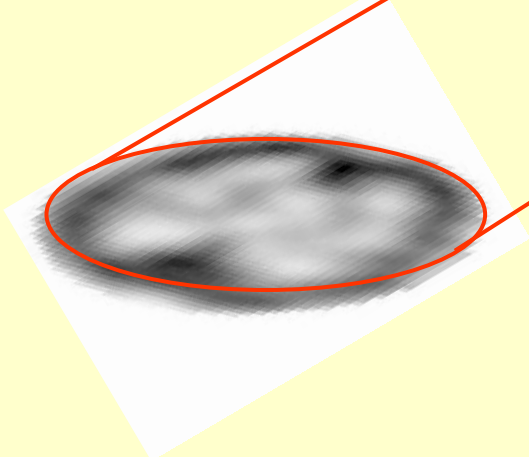
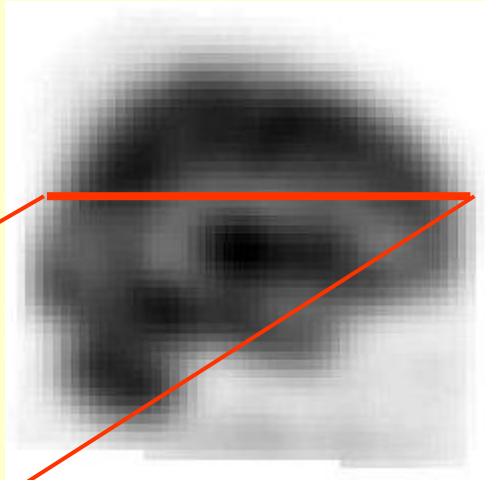
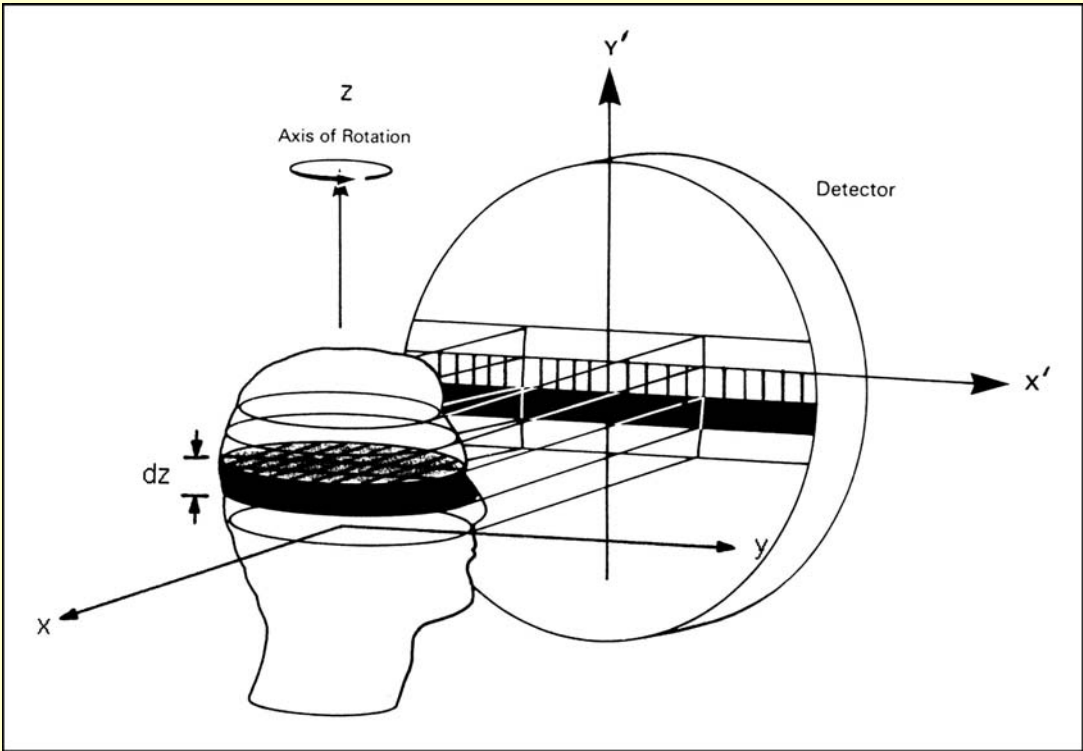
lateral view

courtesy of Dr. K. Kouris

1st step in tomography = recording projections

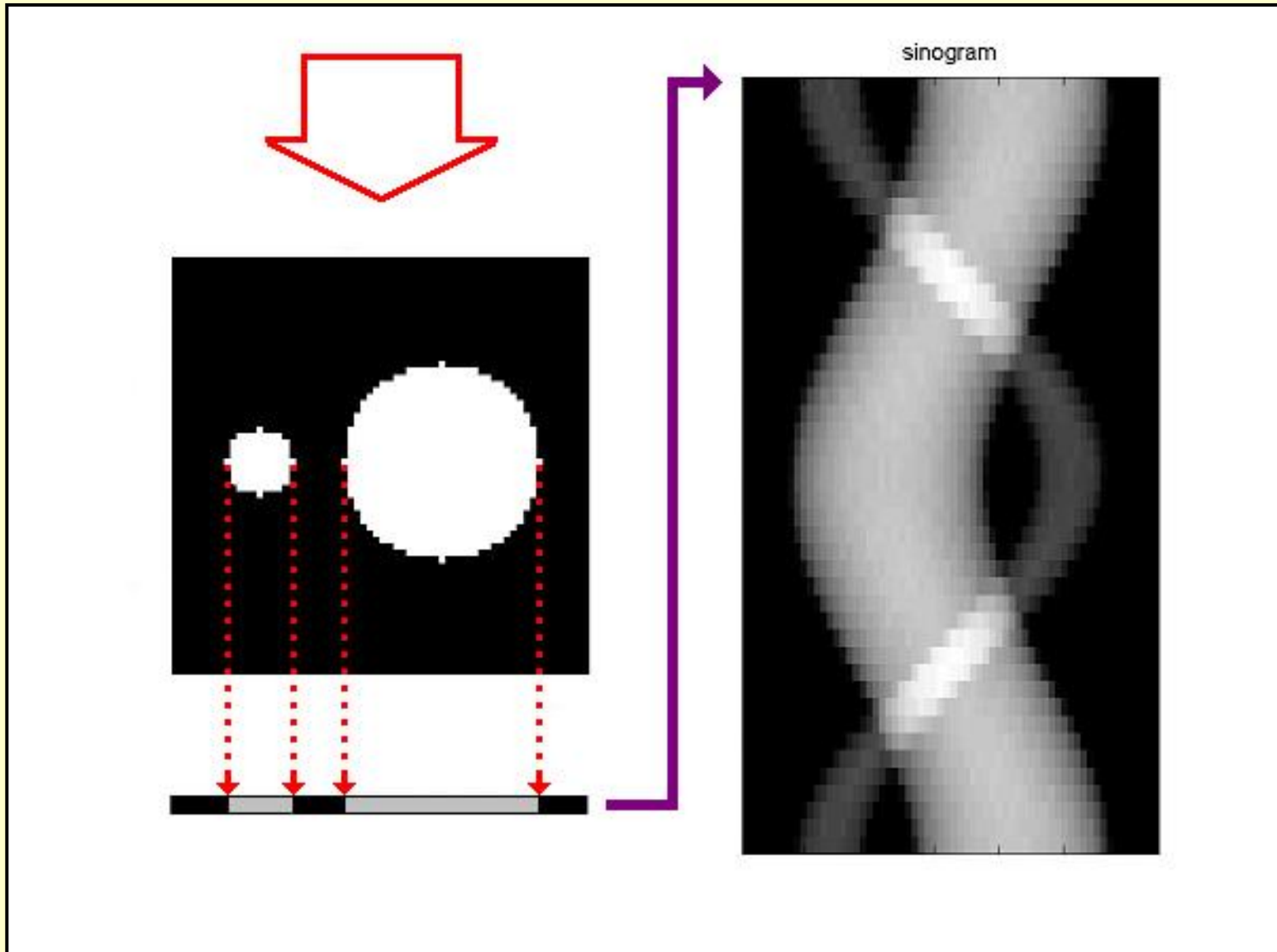


courtesy of Dr. K. Kouris



Groch MW, Erwin WD. J Nucl Med Technol 2000;28:233-244.

Sinogram = collection of projections of a single slice



2nd step in tomography = reconstruction from projections

Analytic reconstruction methods (e.g. the filtered back-projection algorithm) are efficient (fast) and elegant, but they are unable to handle complicated factors such as scatter. Filtered back projection has been used for reconstructions in x-ray CT and for most SPECT and PET reconstructions until recently.

Iterative reconstruction algorithms, on the other hand, are more versatile but less efficient. Efficient (that is - fast) iterative algorithms are currently under development. With rapid increases being made in computer speed and memory, iterative reconstruction algorithms will be used in more and more applications of SPECT and PET and will enable more quantitative reconstructions.

Analytic reconstruction methods

(projection - backprojection algorithms)

filtered back-projection

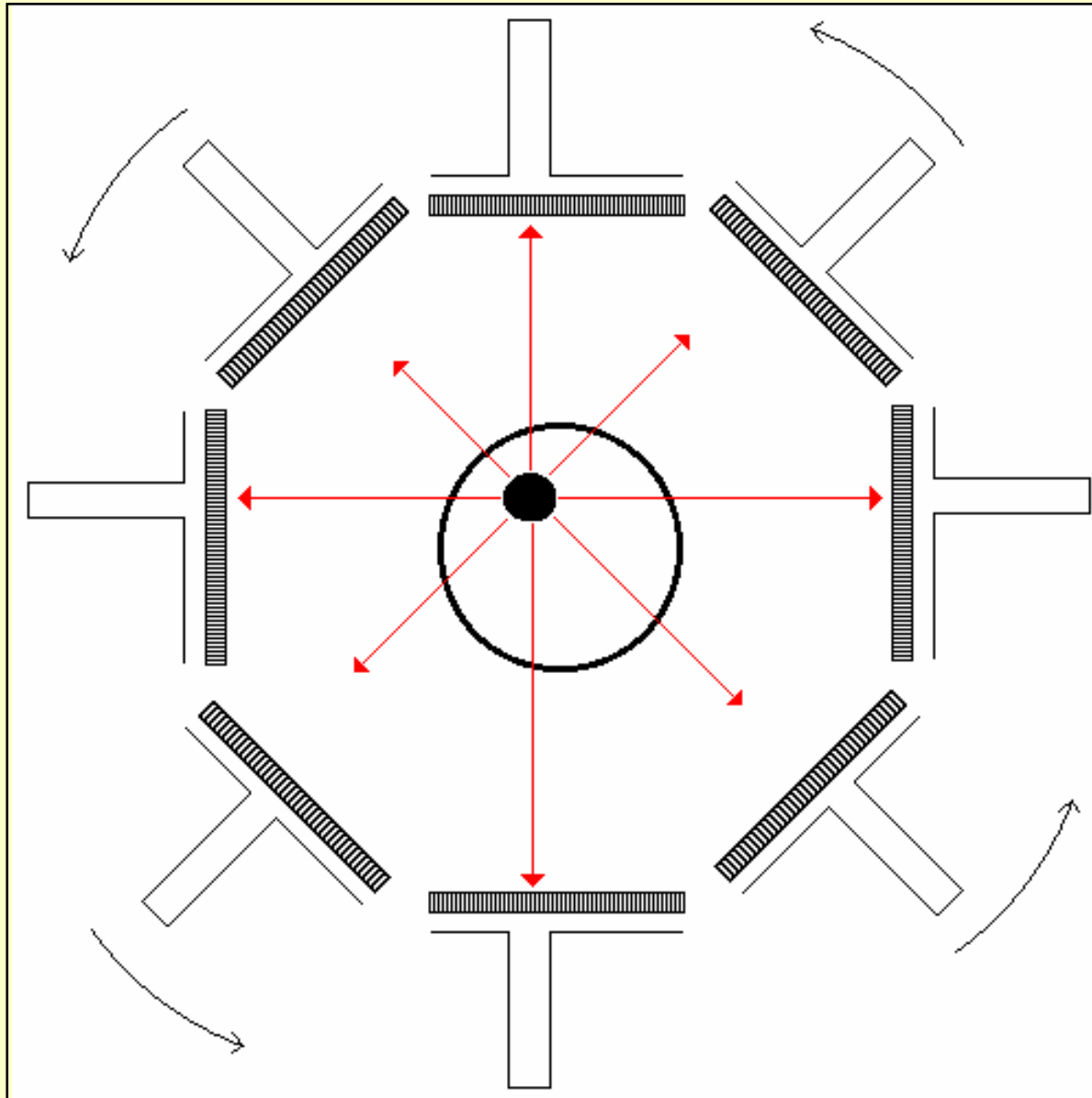
back-projection filtering

Radon J.

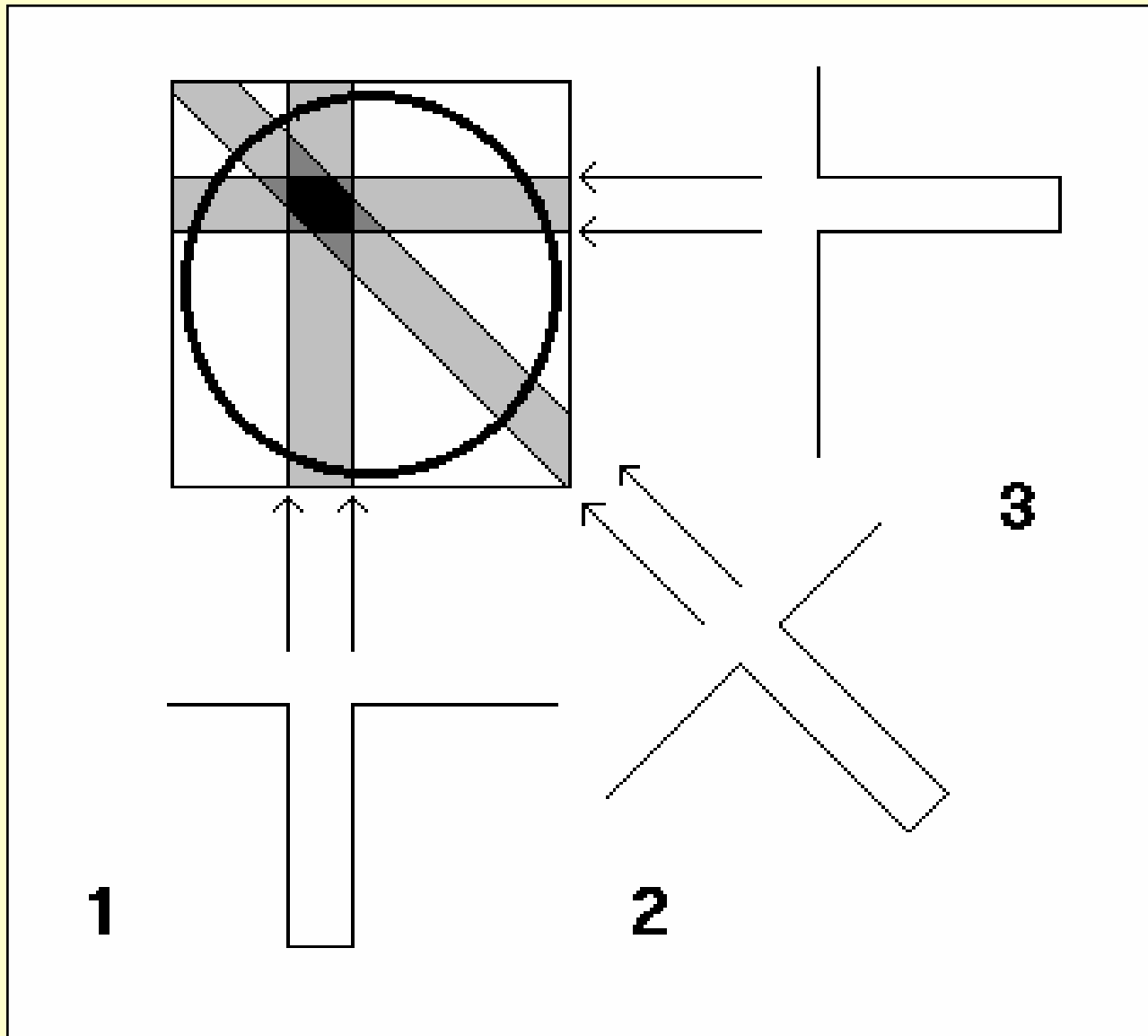
On the determination of functions from their integrals along certain manifolds [in German].

Math Phys Klass 1917;69:262-277.

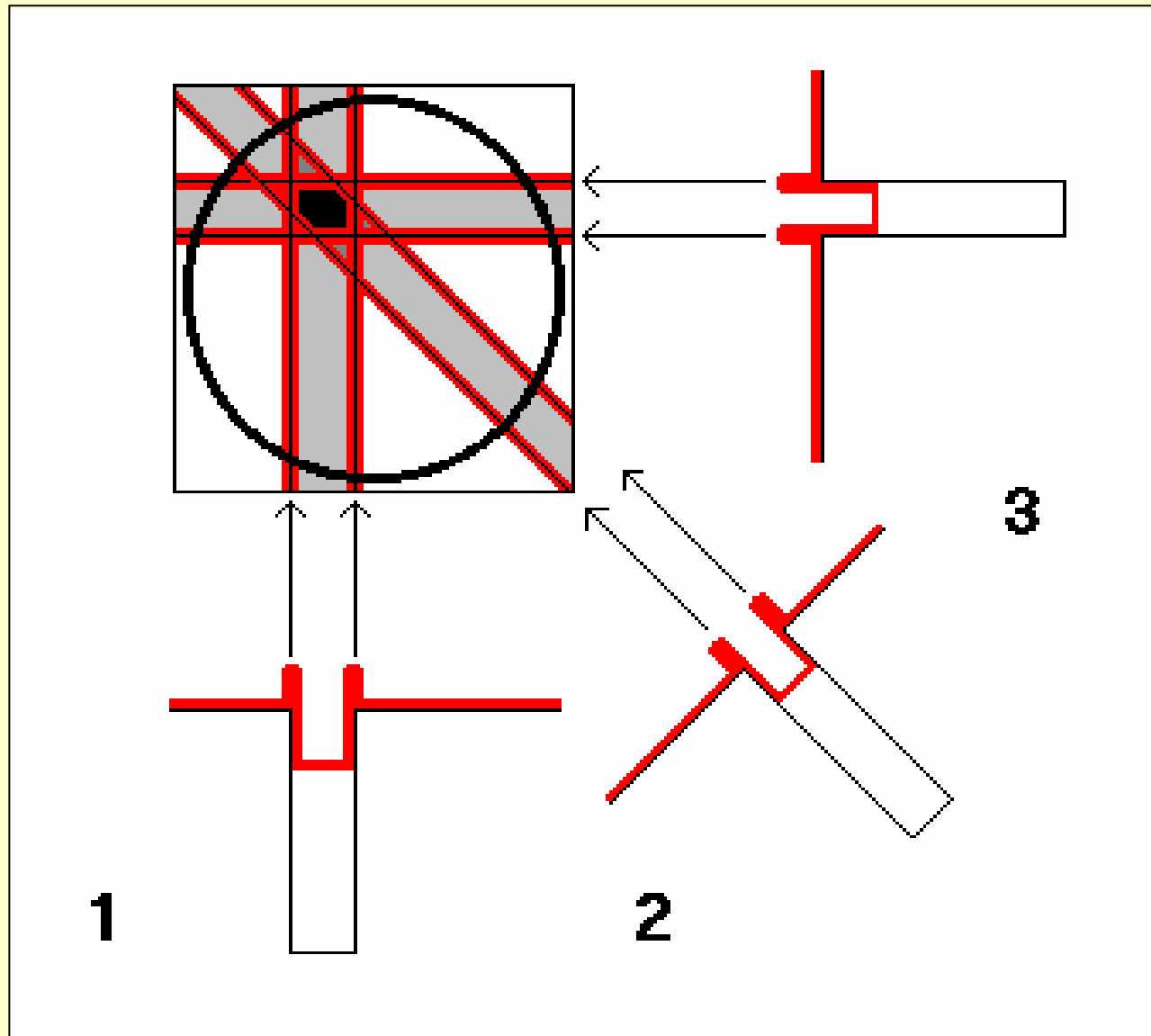
Recording projections of a slice

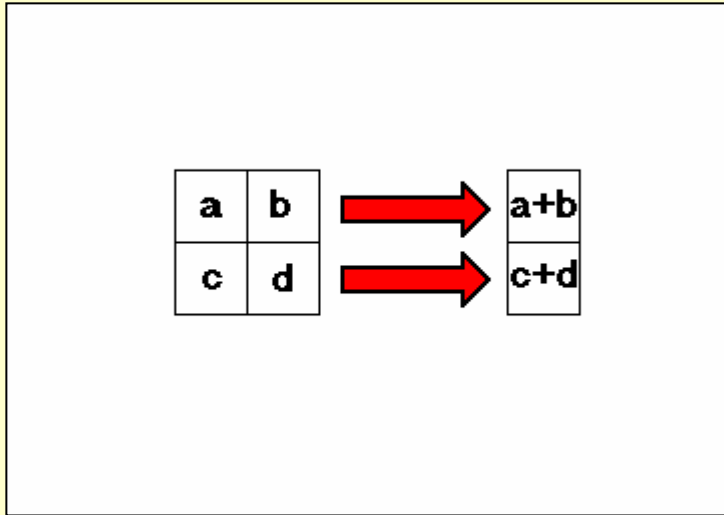


Back projection (BP)

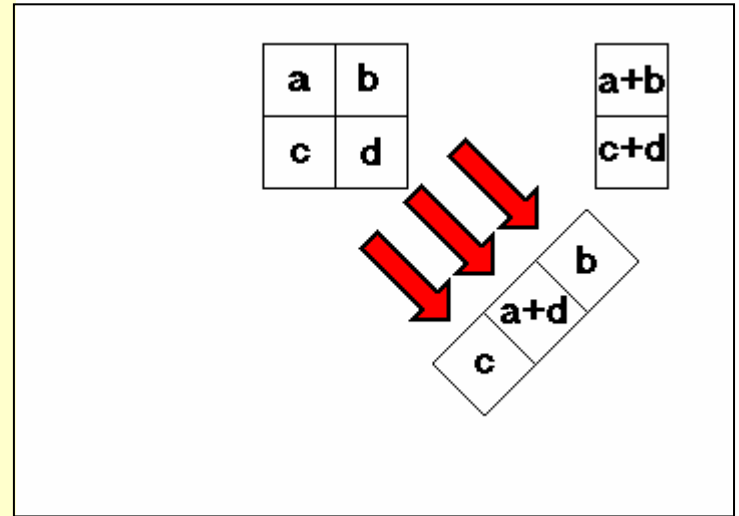


Filtered back-projection (FBP)

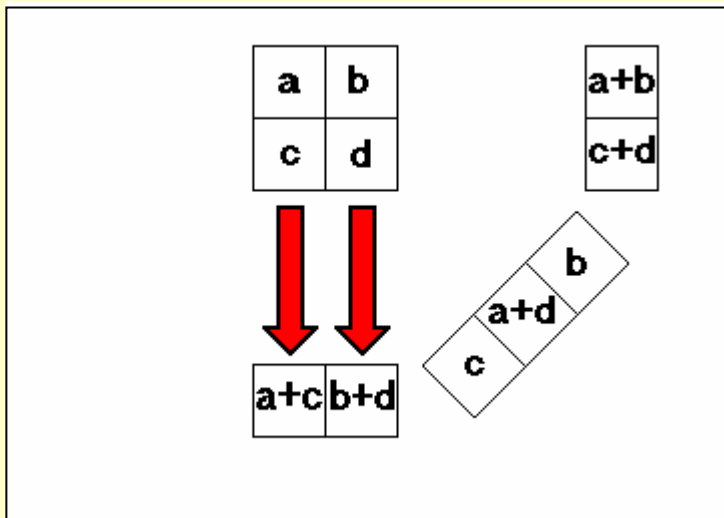




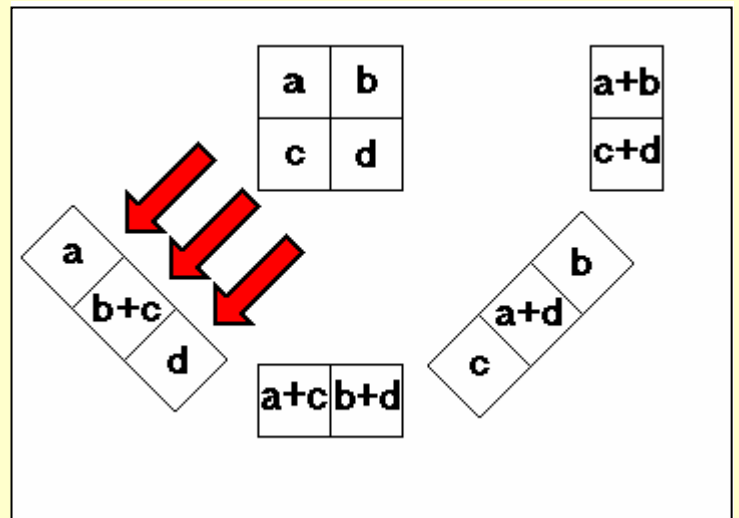
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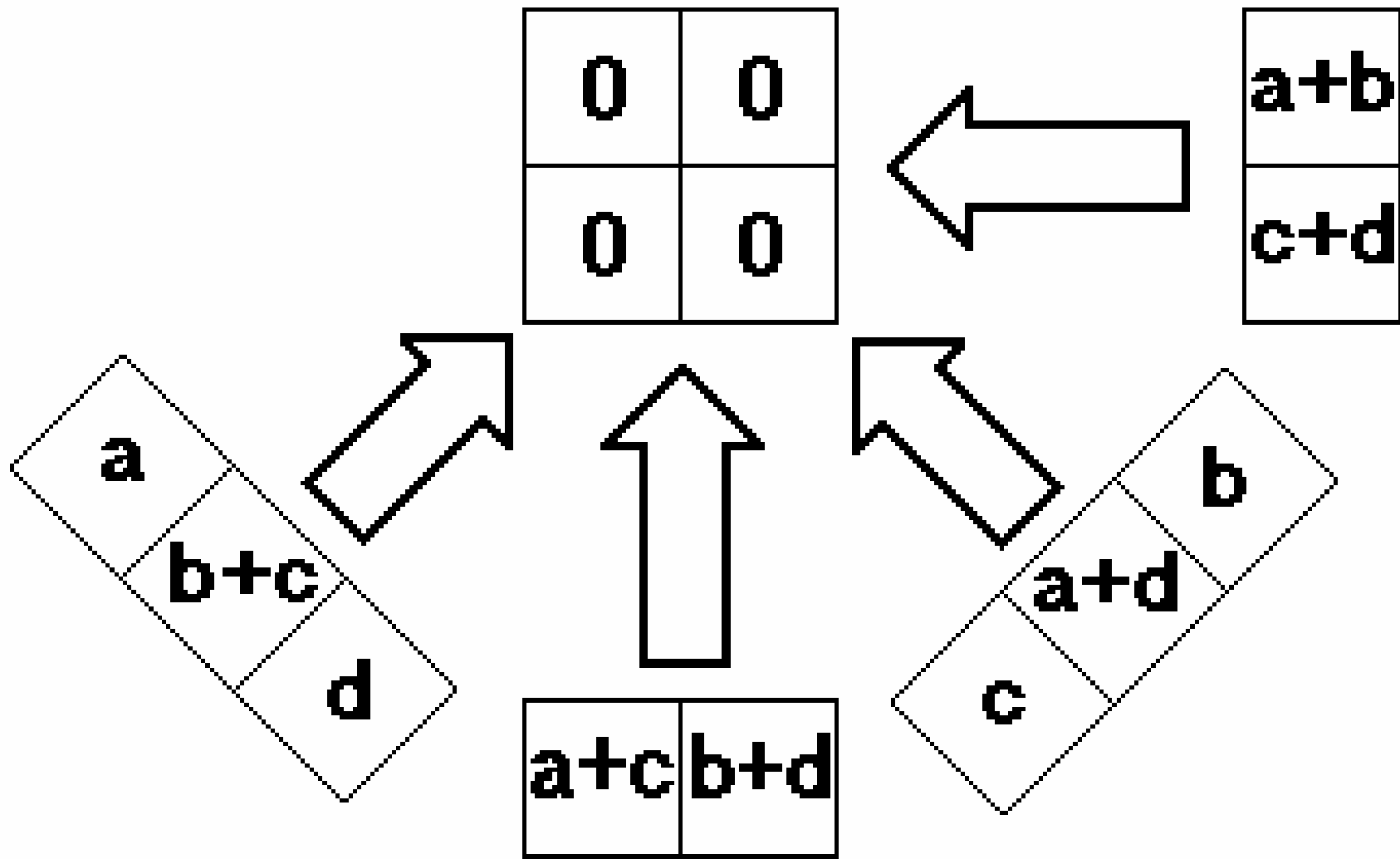
2

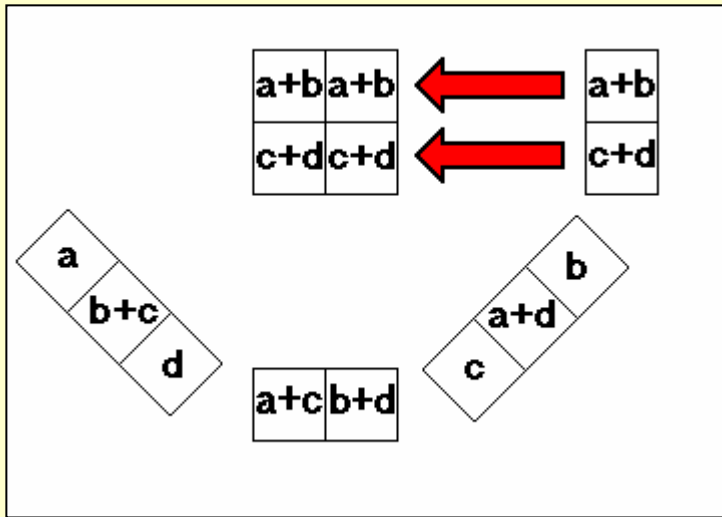


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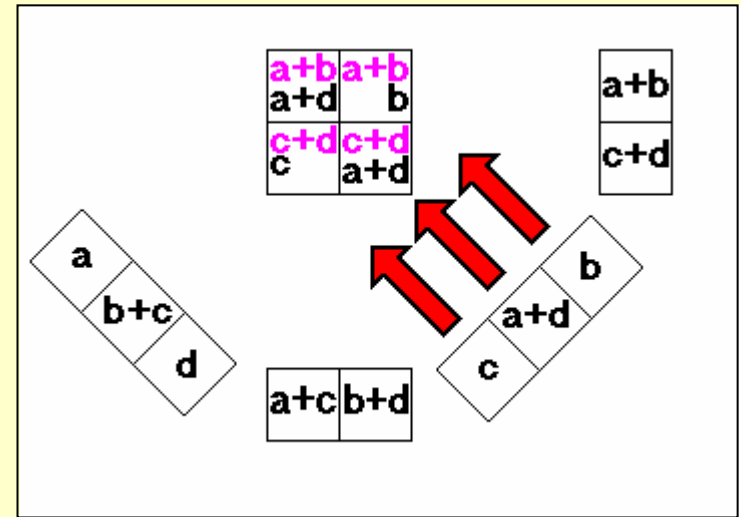


4

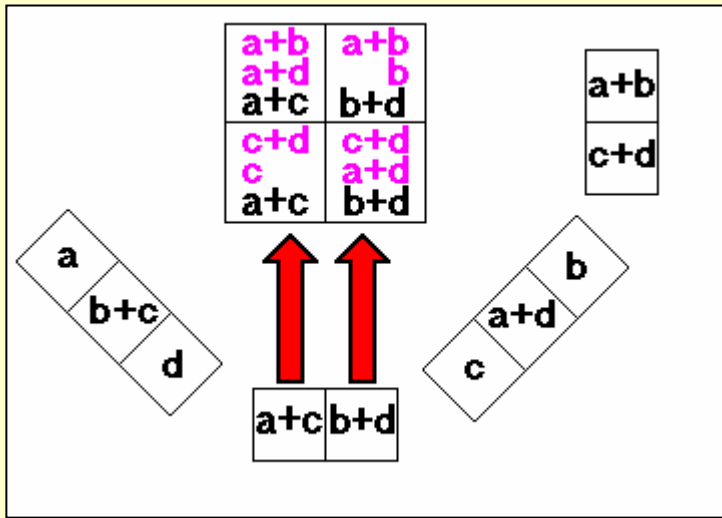




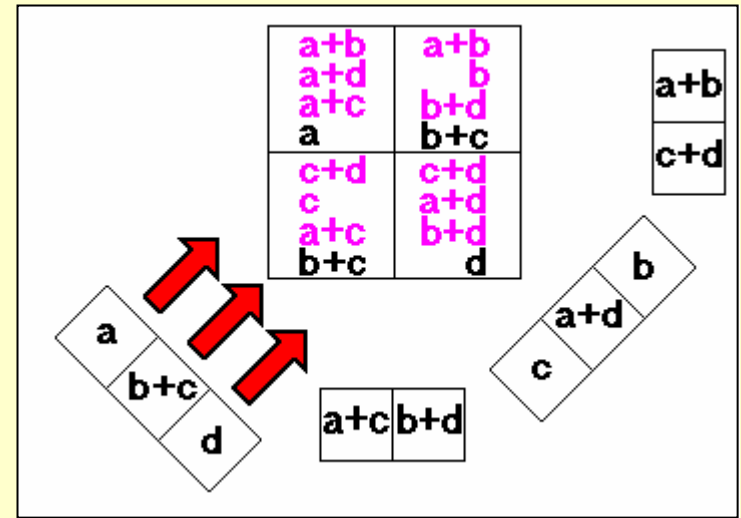
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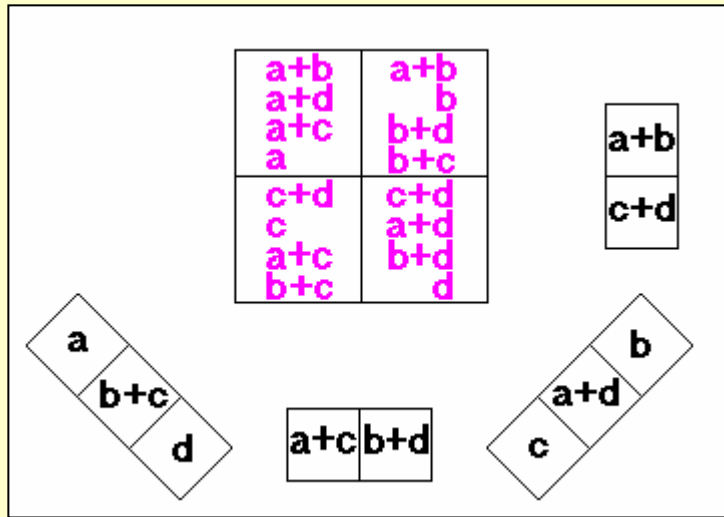
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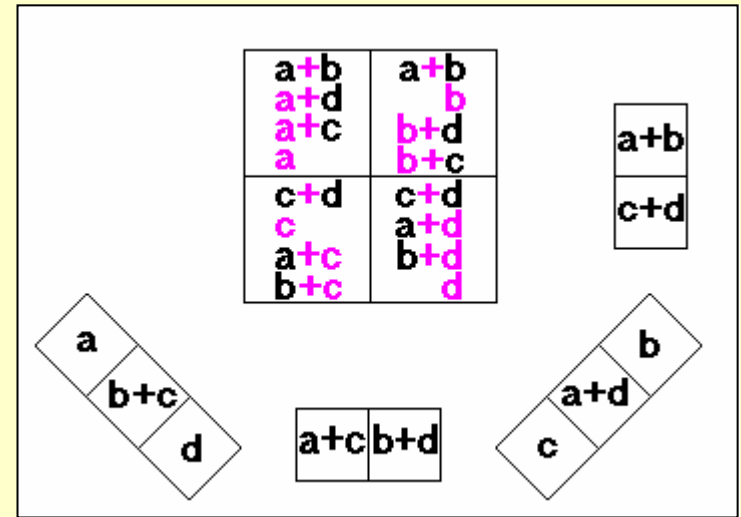
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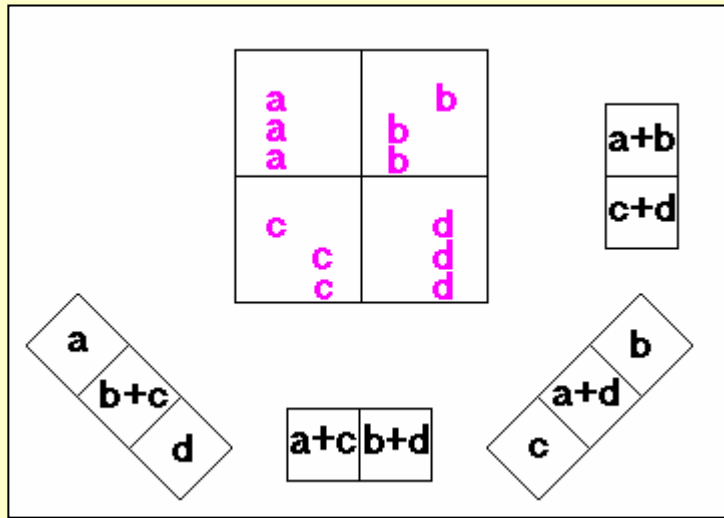
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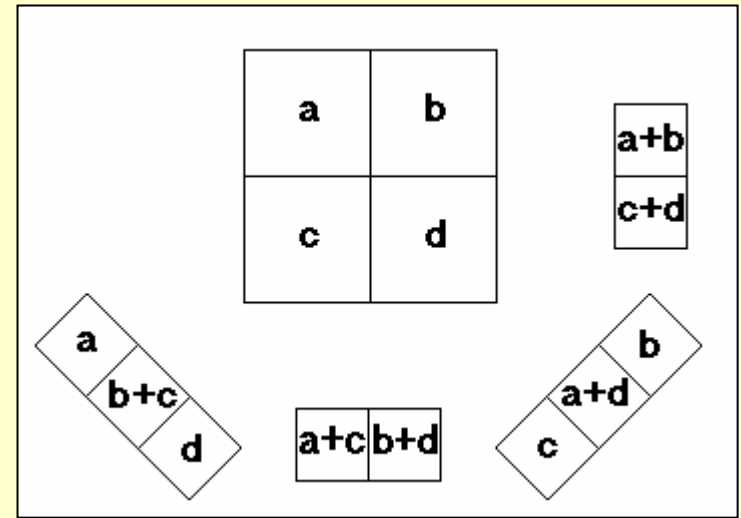
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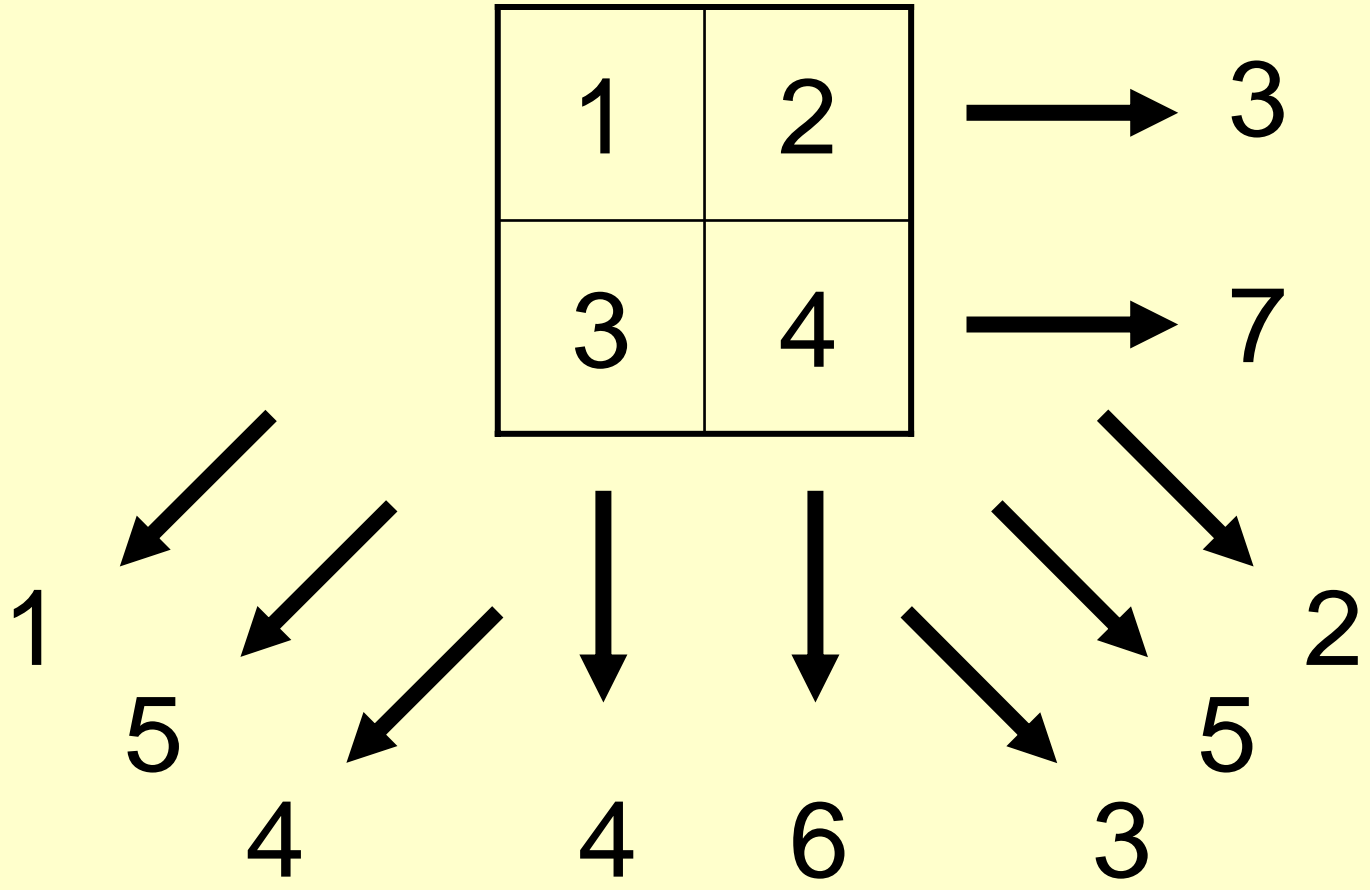
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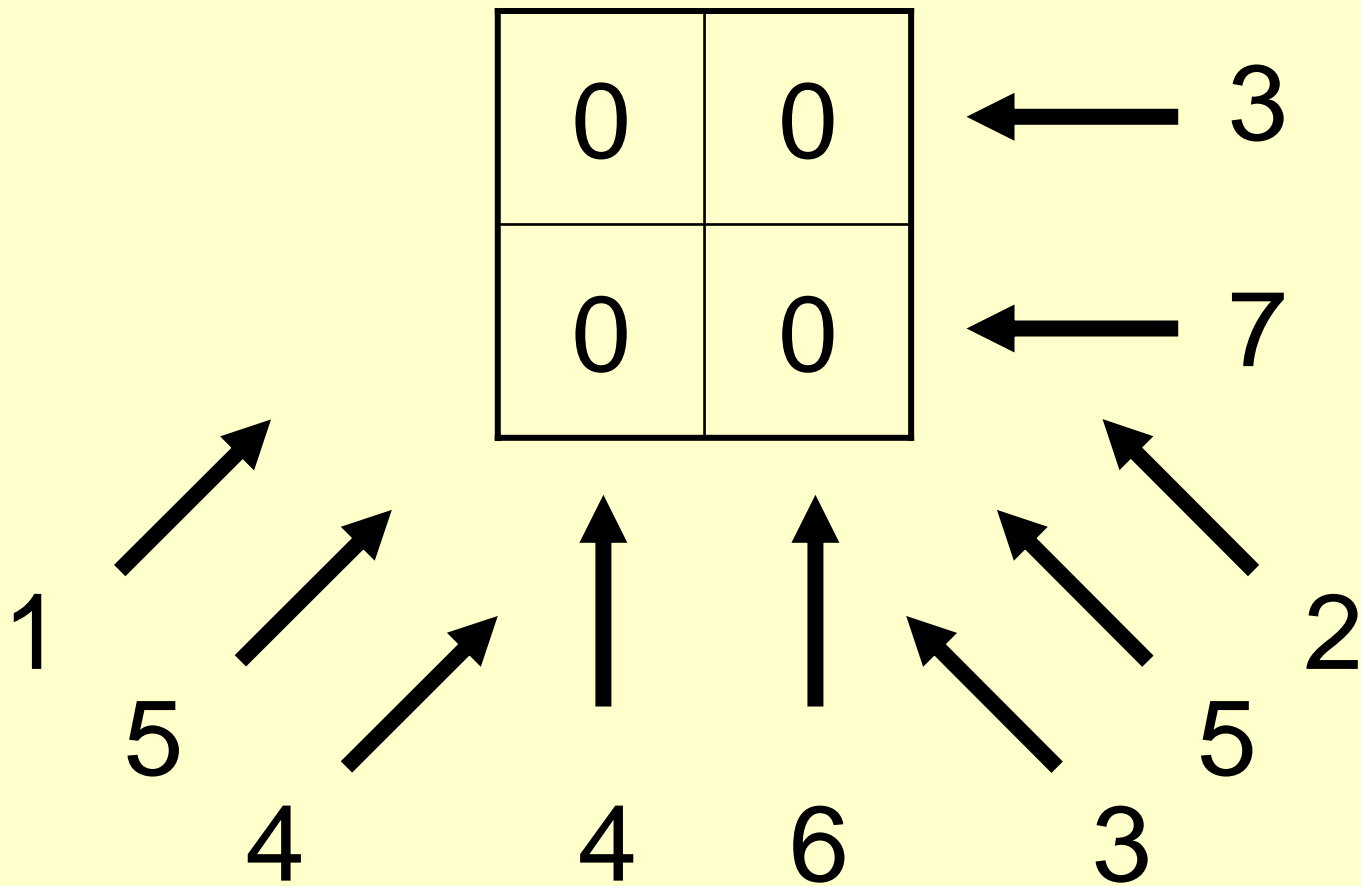


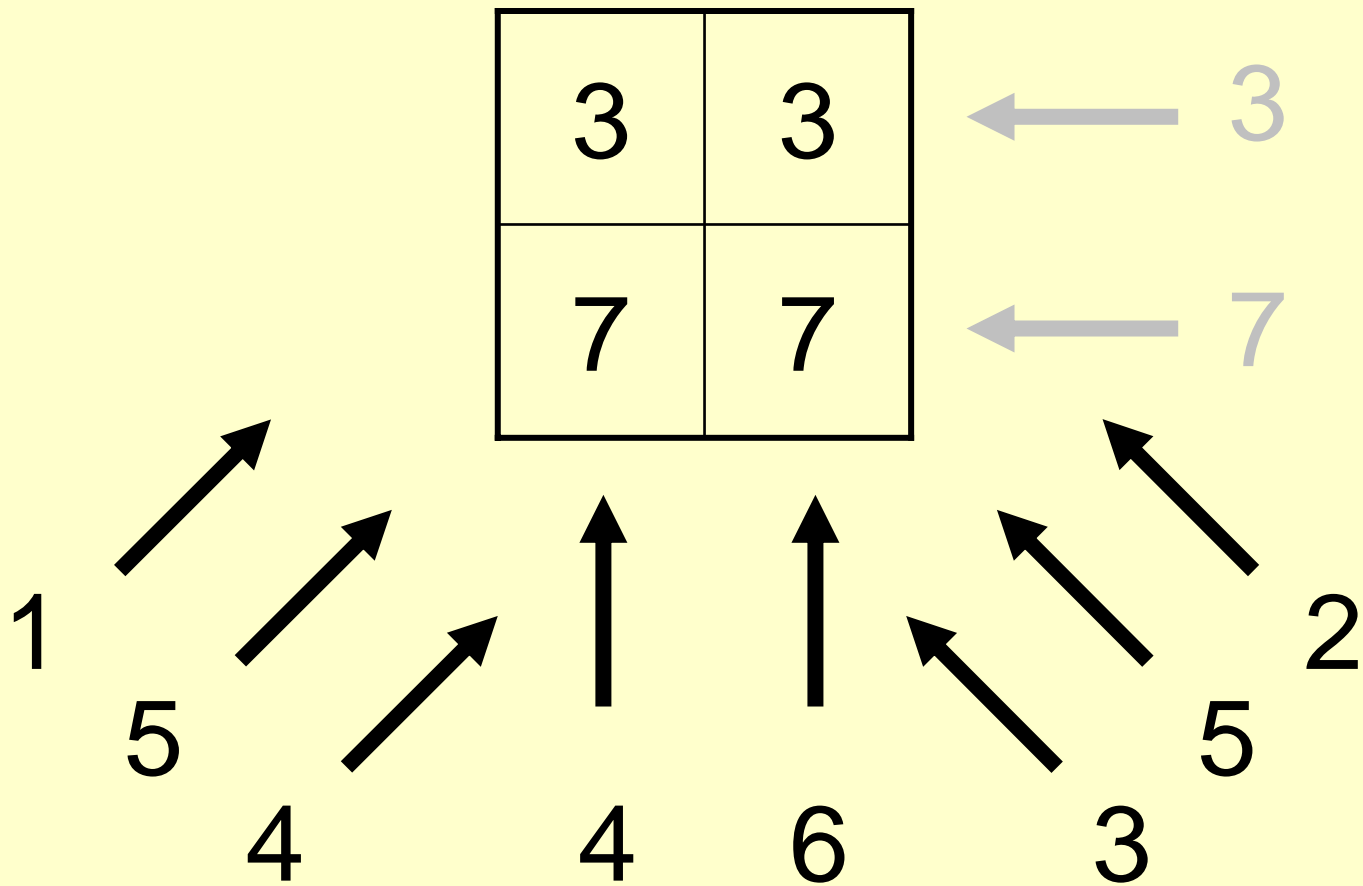
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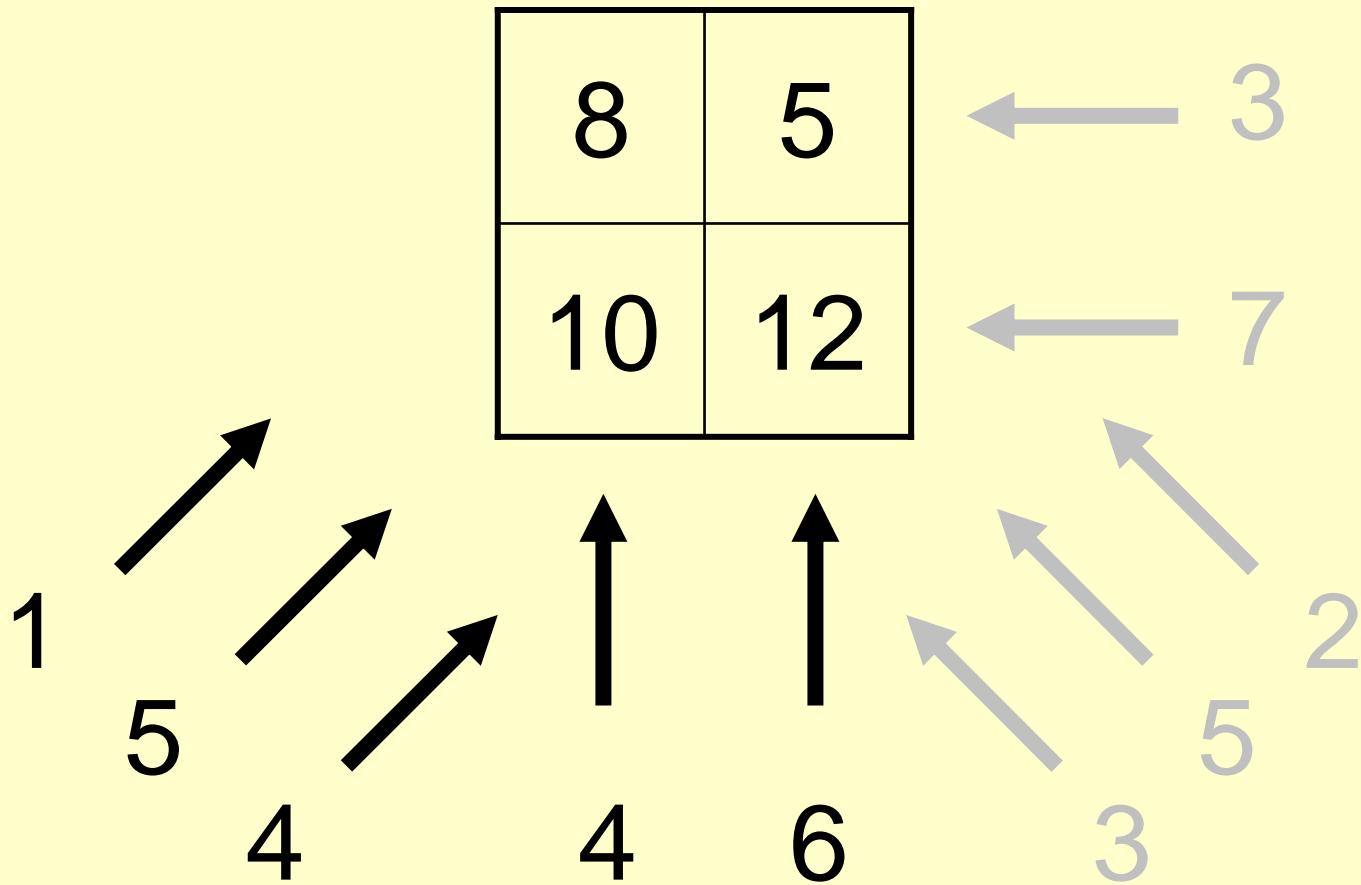


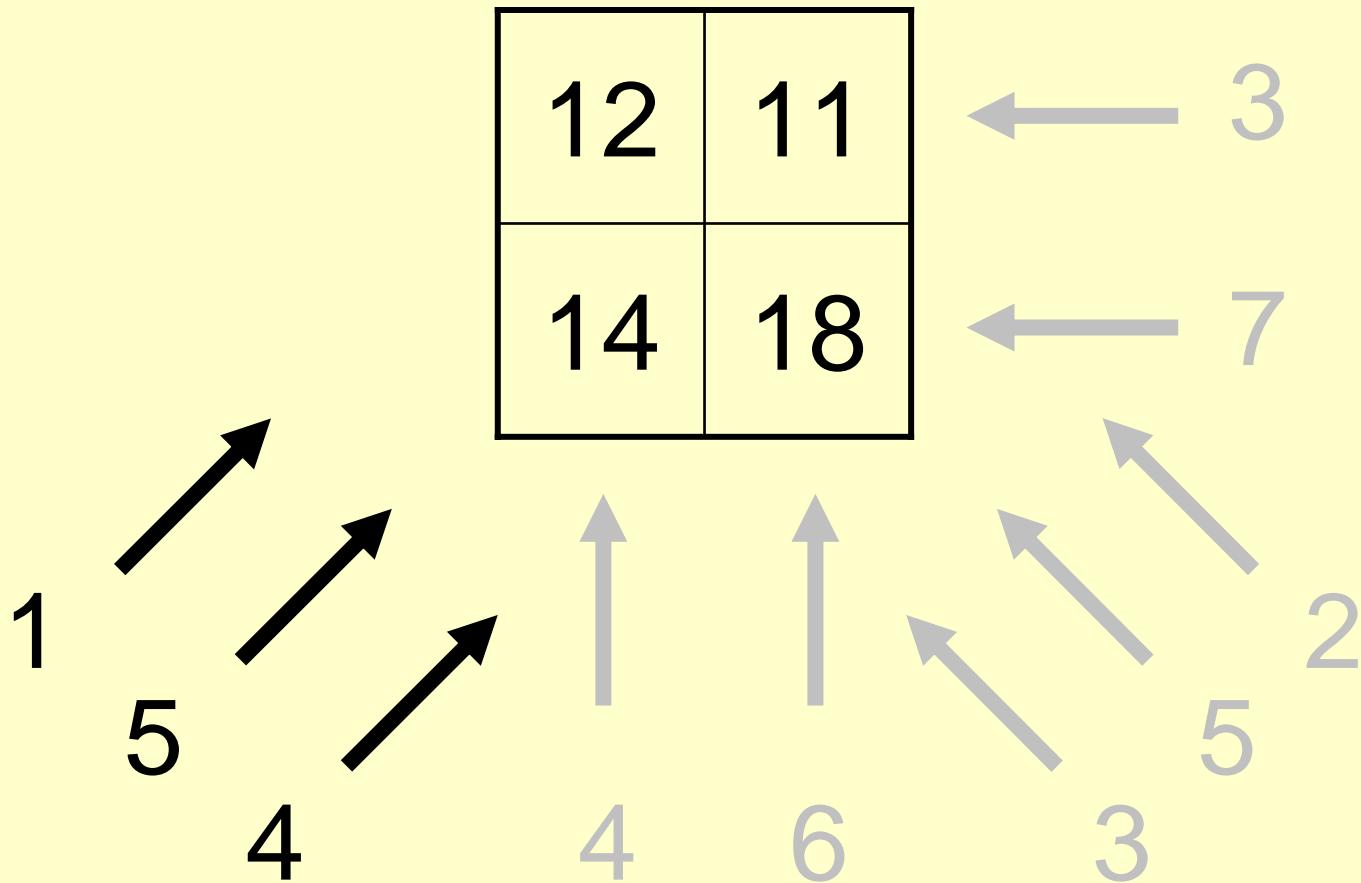
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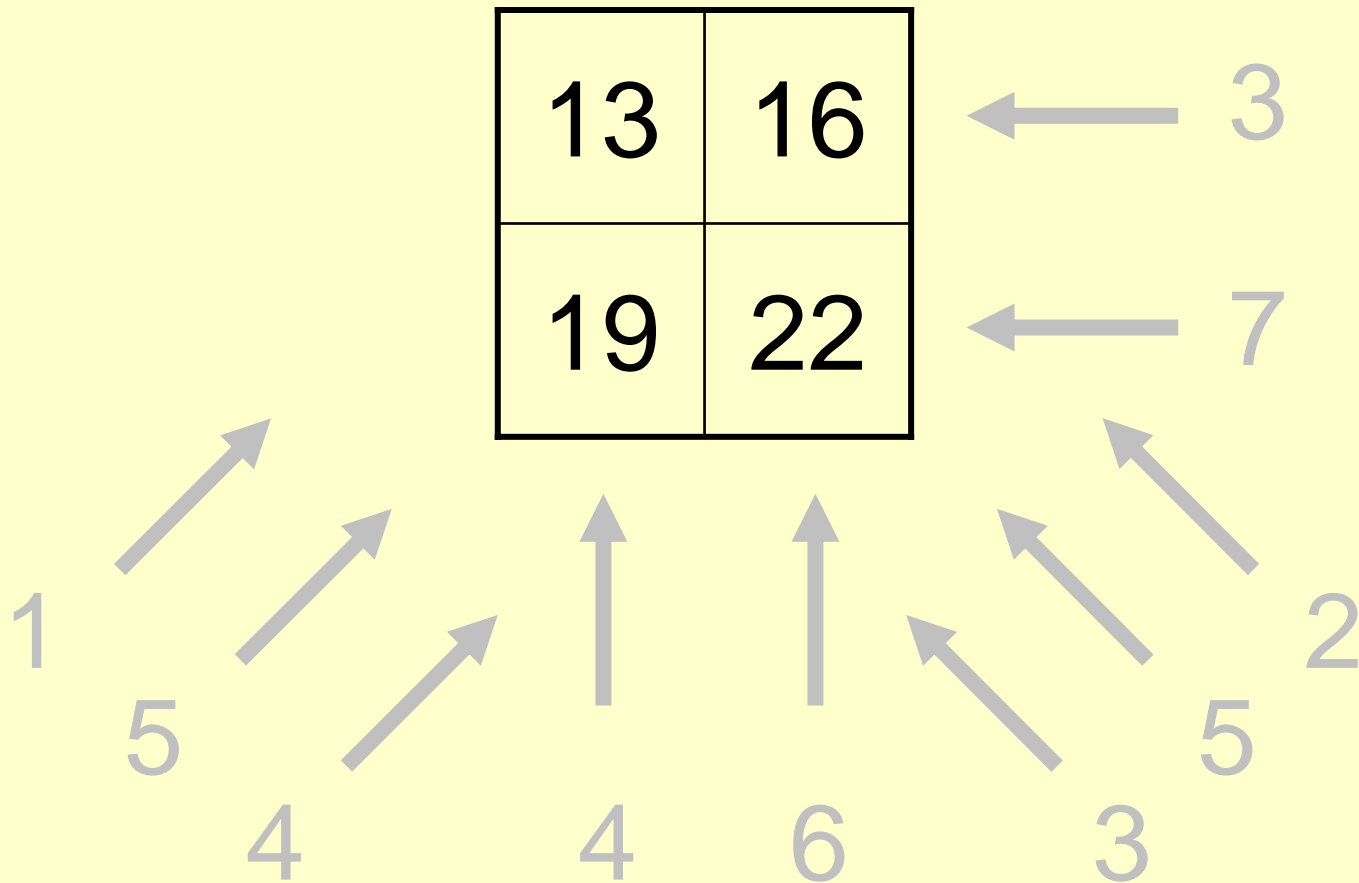




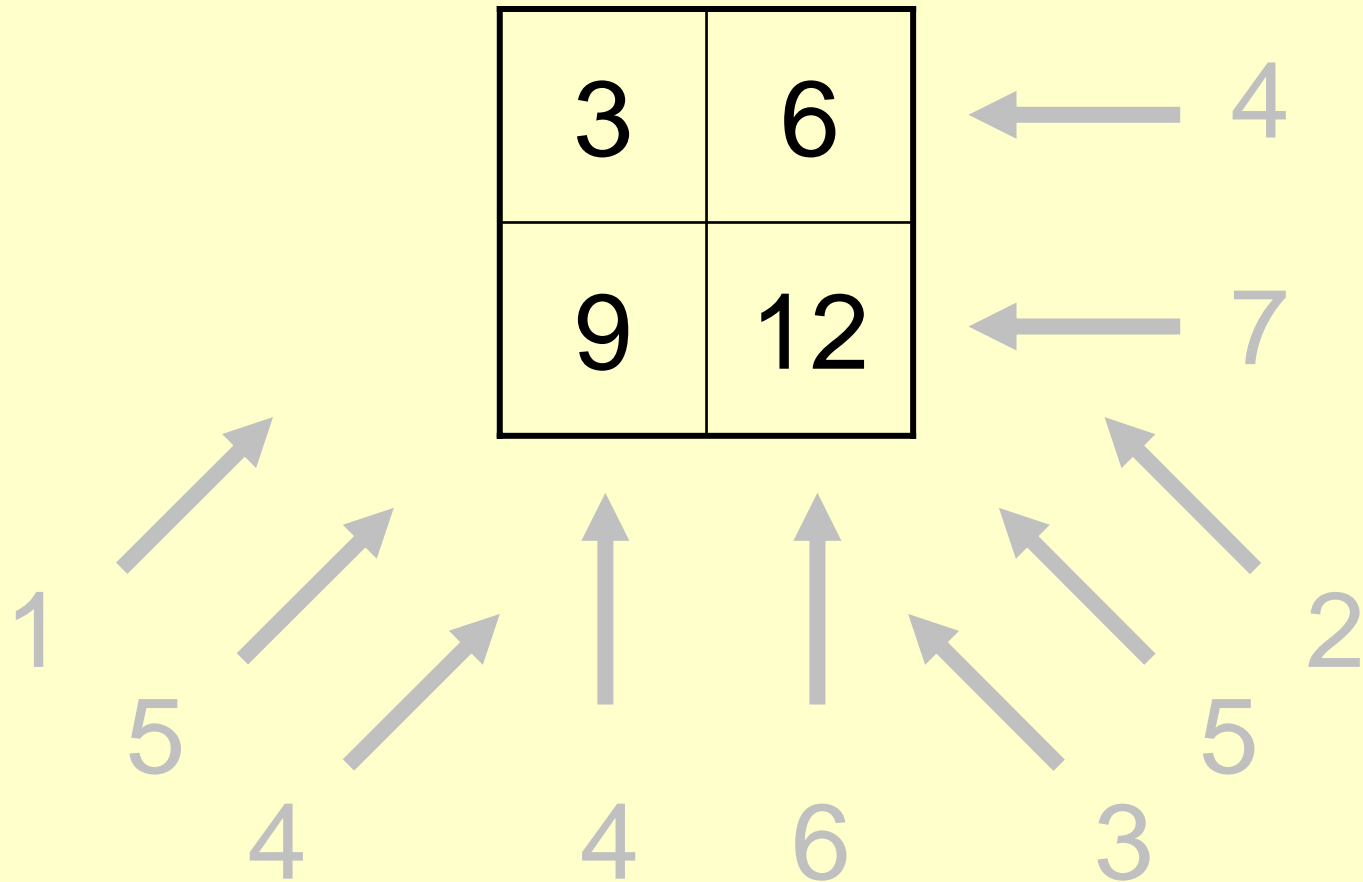


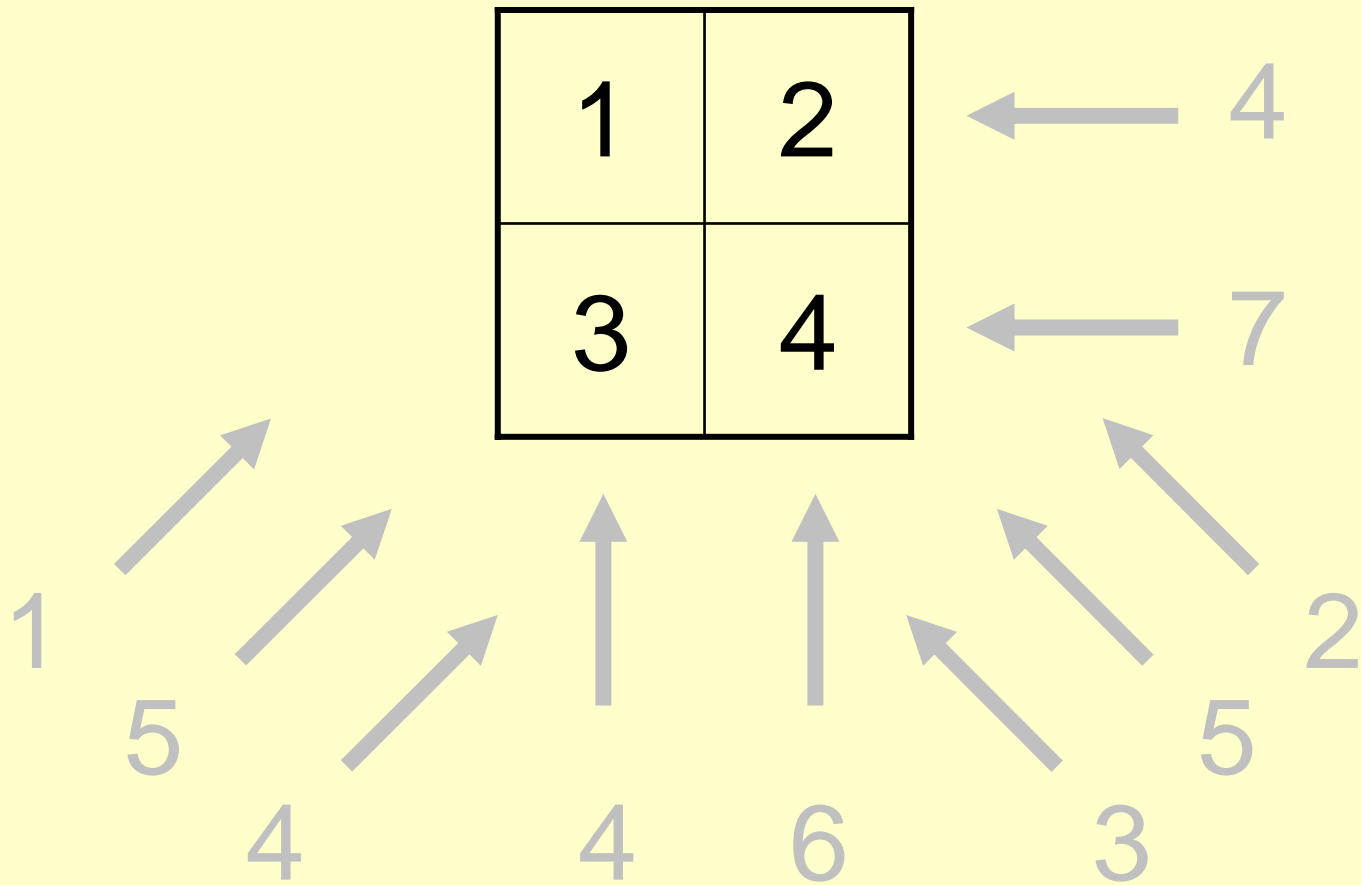


- 10 (subtract total sum from each entry)

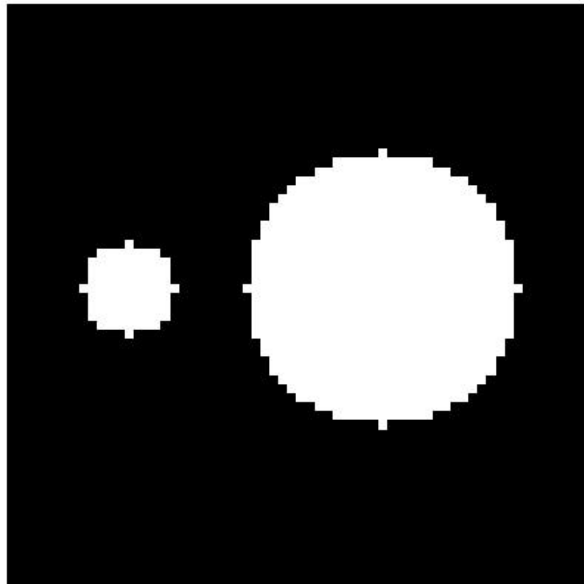


/ 3 (divide each entry by 3)

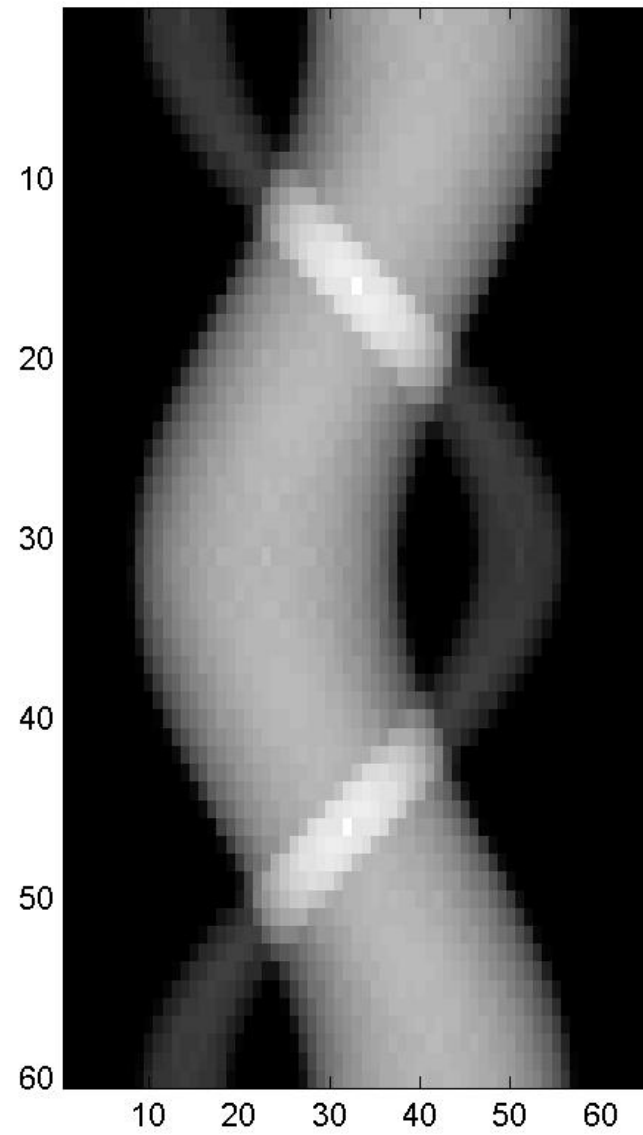




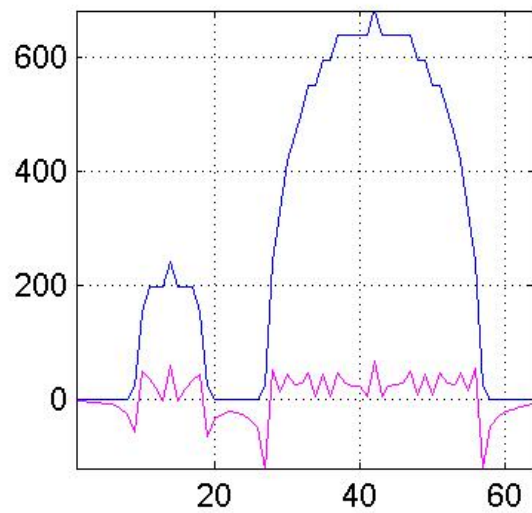
original slice



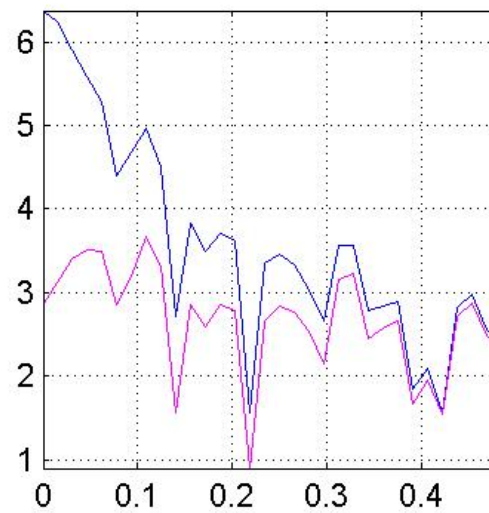
sinogram



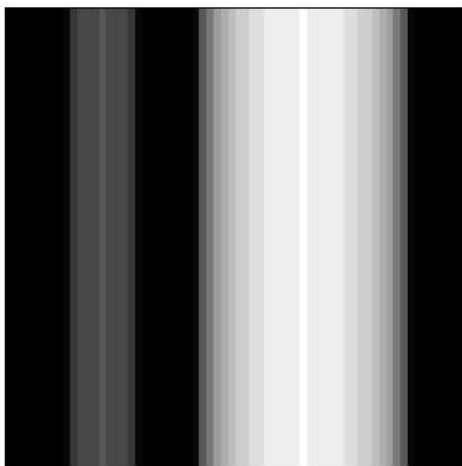
profile at angle 0 deg



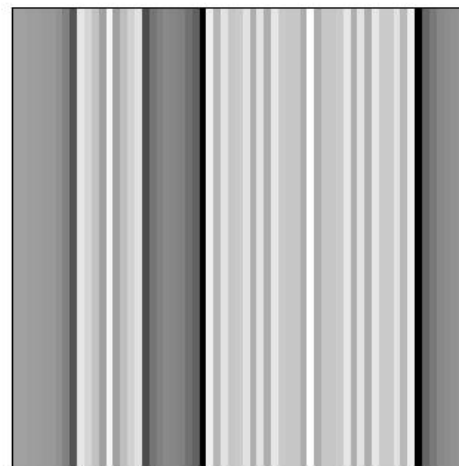
projection spectra

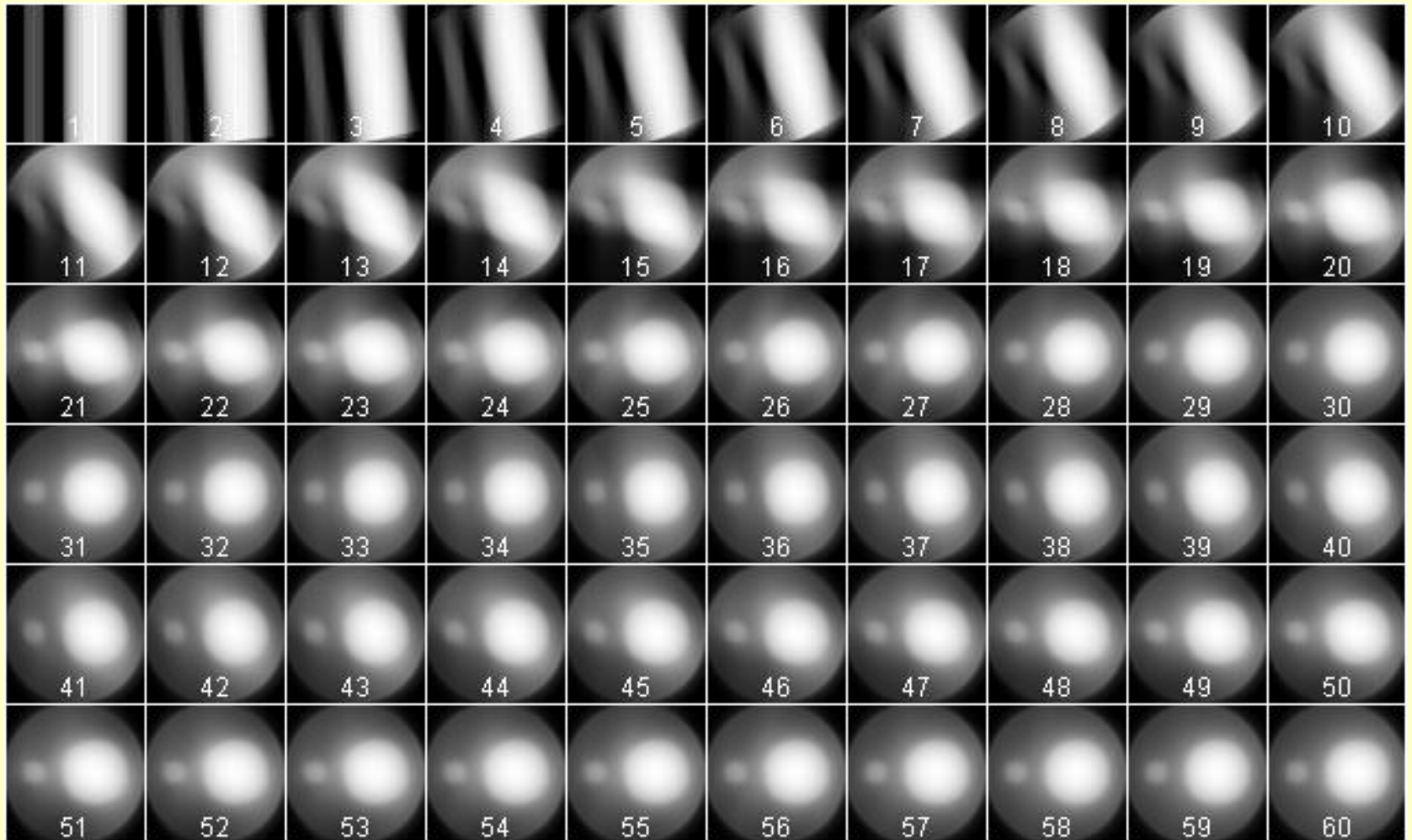


backprojection

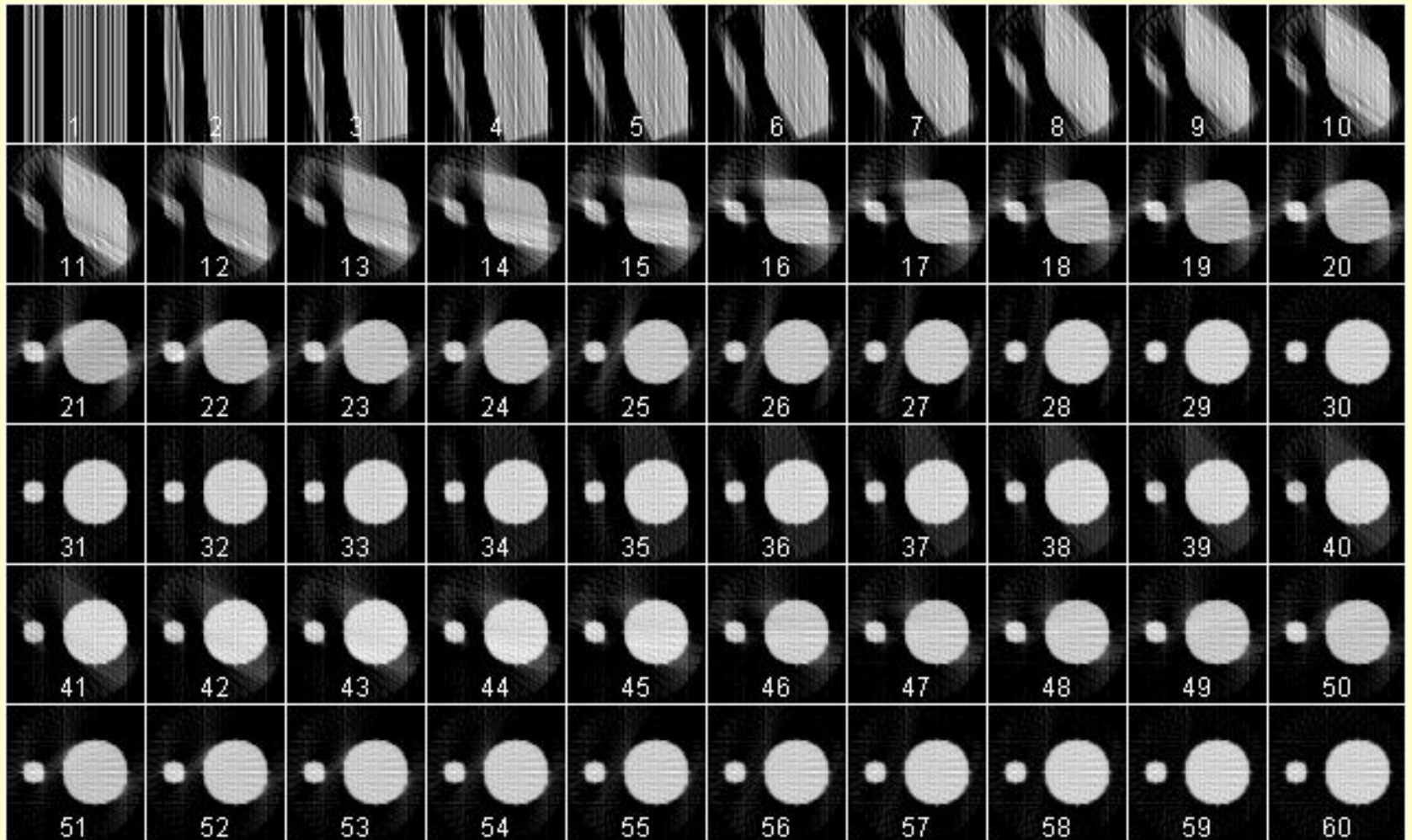


filtered



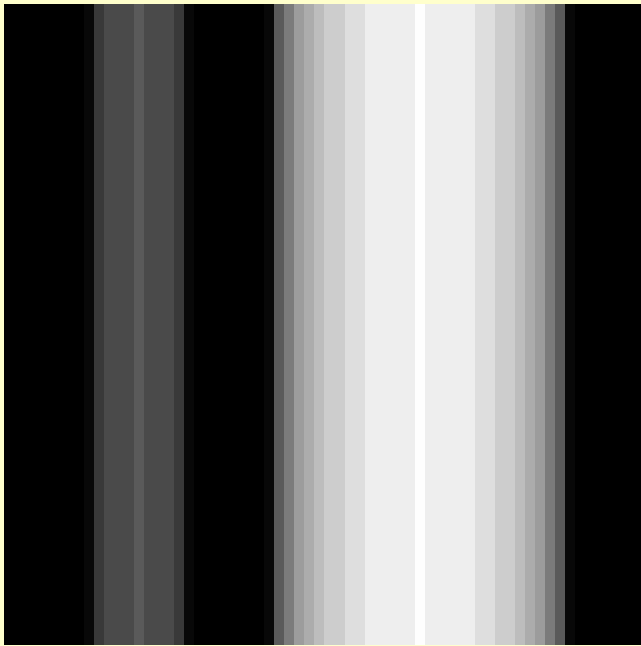


back projection (BP) = summation of projections

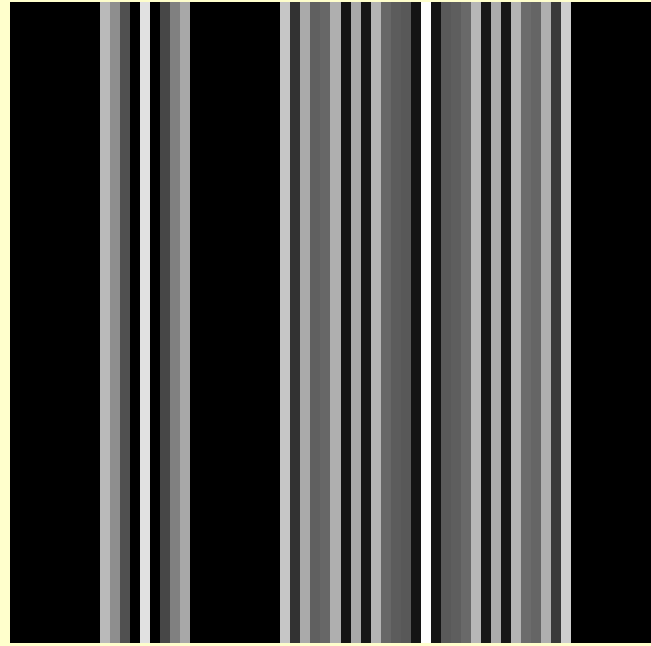


filtered back projection (FBP)

Sequence of summing original and filtered projections



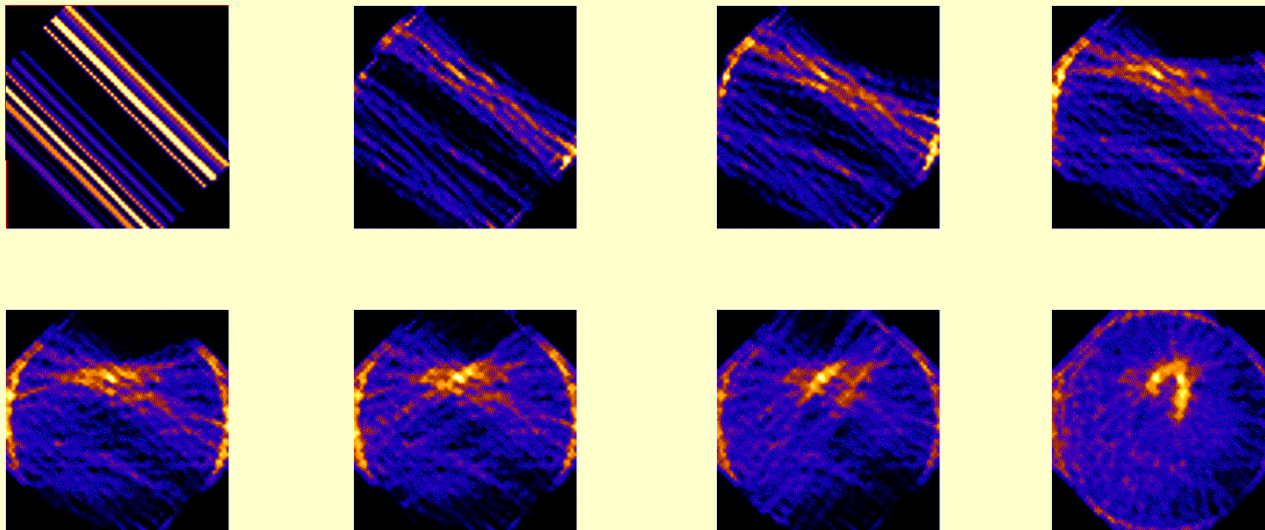
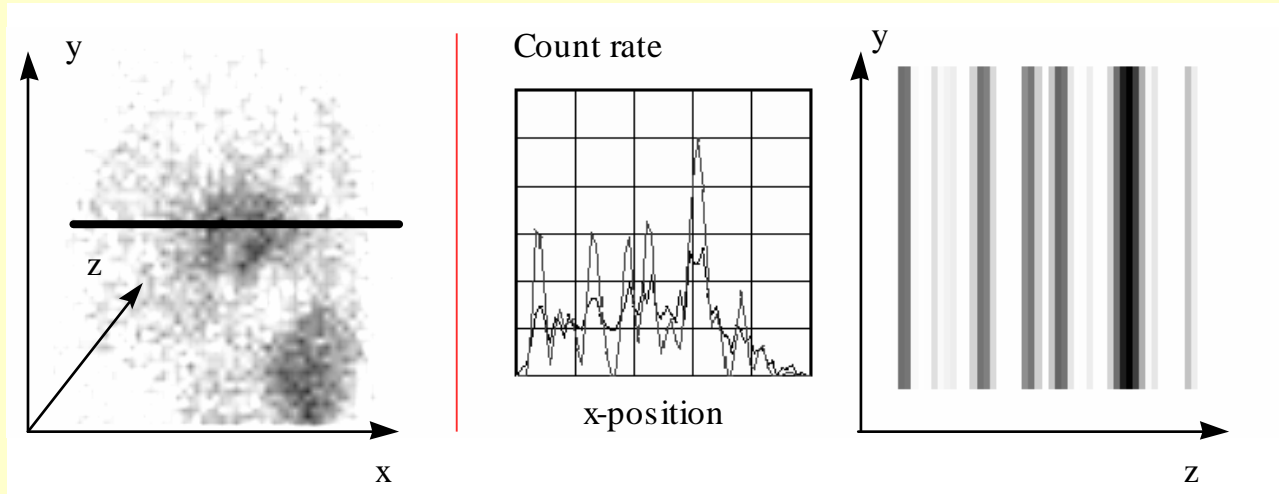
back projection



filtered back projection

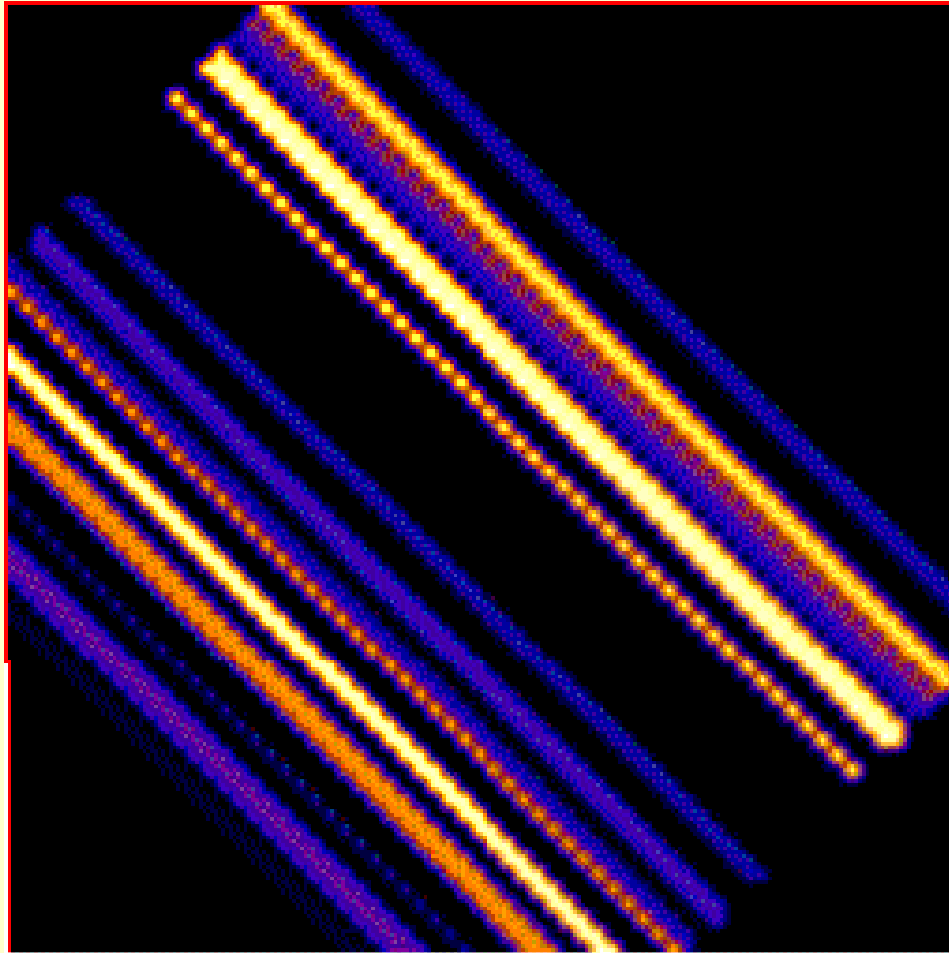
Reconstruction of a slice from projections

example = myocardial perfusion, left ventricle, long axis



courtesy of Dr. K. Kouris

Reconstruction of a slice from projections
example = myocardial perfusion, left ventricle, long axis



courtesy of Dr. K. Kouris

Iterative reconstruction methods

conventional iterative algebraic methods

algebraic reconstruction technique (ART)
simultaneous iterative reconstruction technique (SIRT)
iterative least-squares technique (ILST)

iterative statistical reconstruction methods (with and without using a priori information)

gradient and conjugate gradient (CG) algorithms
maximum likelihood expectation maximization (MLEM)
ordered-subsets expectation maximization (OSEM)
maximum a posteriori (MAP) algorithms

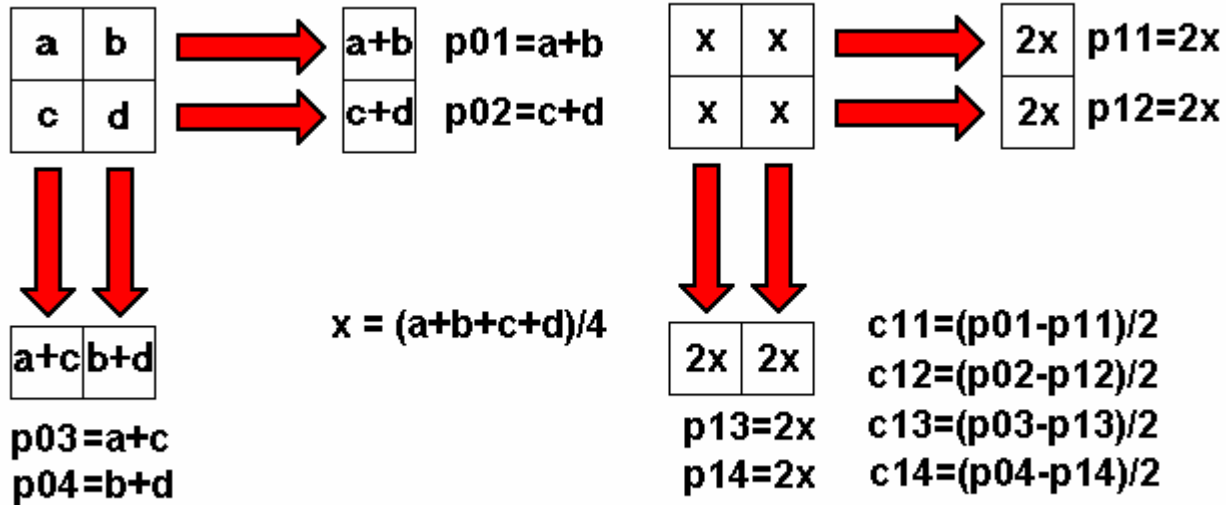
The principle of the iterative algorithms is to find a solution (that is - to reconstruct an image of a tomographic slice from projections) by **successive estimates**. The projections corresponding to the current estimate are compared with the measured projections. The result of the comparison is used to modify the current estimate, thereby creating a new estimate.

The algorithms differ in the way the measured and estimated projections are compared and the kind of correction applied to the current estimate. The process is initiated by arbitrarily creating a first estimate - for example, a uniform image (all pixels equal zero, one, or a mean pixel value,...). Corrections are carried out either as addition of differences or multiplication by quotients between measured and estimated projections.

algorithm (a recipe)

- (1) make the first arbitrary estimate of the slice (homogeneous image),
- (2) project the estimated slice into projections analogous to those measured by the camera (**important:** in this step, physical corrections can be introduced - for attenuation, scatter, and depth-dependent collimator resolution),
- (3) compare the projections of the estimate with measured projections (subtract or divide the corresponding projections in order to obtain correction factors - in the form of differences or quotients),
- (4) stop or continue: if the correction factors are approaching zero, if they do not change in subsequent iterations, or if the maximum number of iterations was achieved, then finish; otherwise
- (5) apply corrections to the estimate (add the differences to individual pixels or multiply pixel values by correction quotients) - thus make the new estimate of the slice,
- (6) go to step (2).

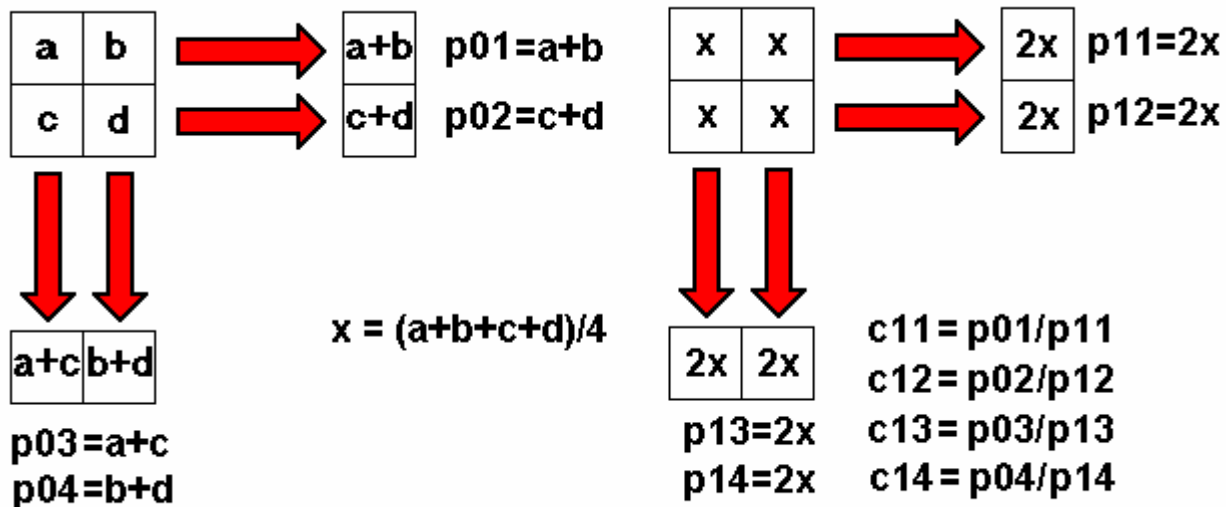
measured
projections



first estimate
and its
projections

correction
factors
(differences
between
projections)

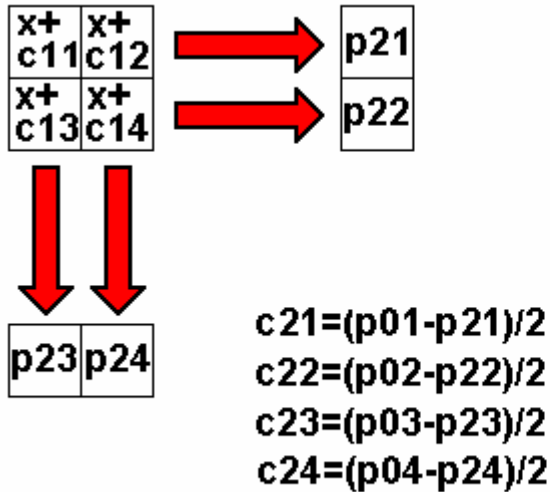
measured
projections



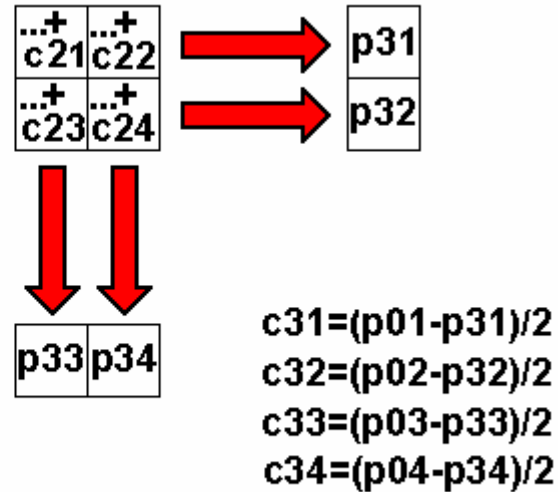
first estimate
and its
projections

correction
factors
(quotients
between
projections)

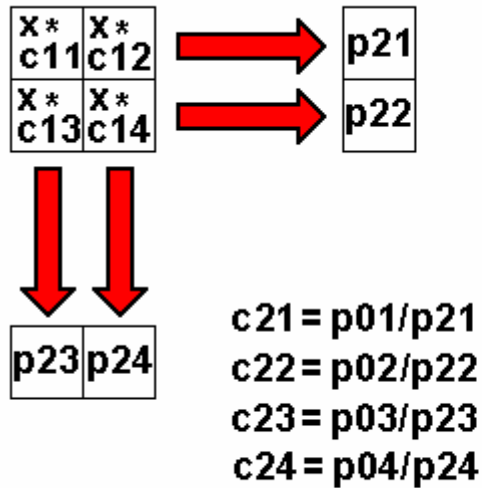
first iteration
(additive corrections)



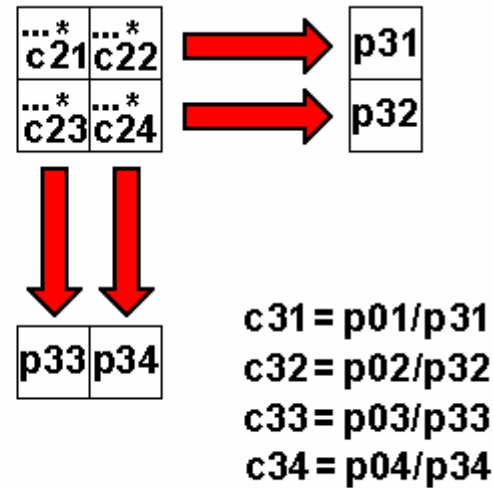
second iteration
(additive corrections)

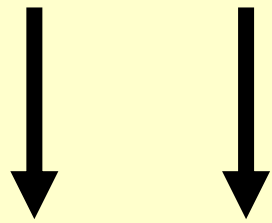
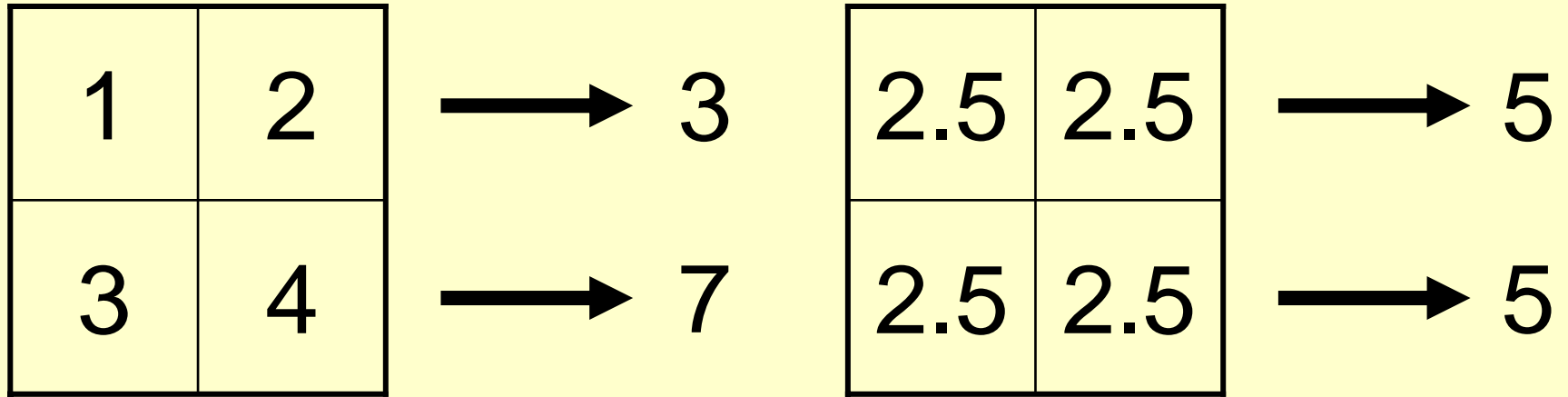


first iteration
(multiplicat. corrections)

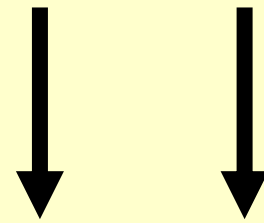


second iteration
(multiplicat. corrections)





4 6



5 5

$$c_{11} = (3 - 5)/2 + (4 - 5)/2 = -2/2 - 1/2$$

$$c_{11} = -1 - 0.5 = -1.5$$

1	2
3	4

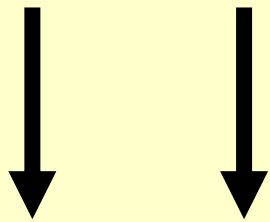
→ 3

→ 7

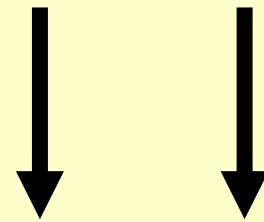
2.5	2.5
2.5	2.5

→ 5

→ 5



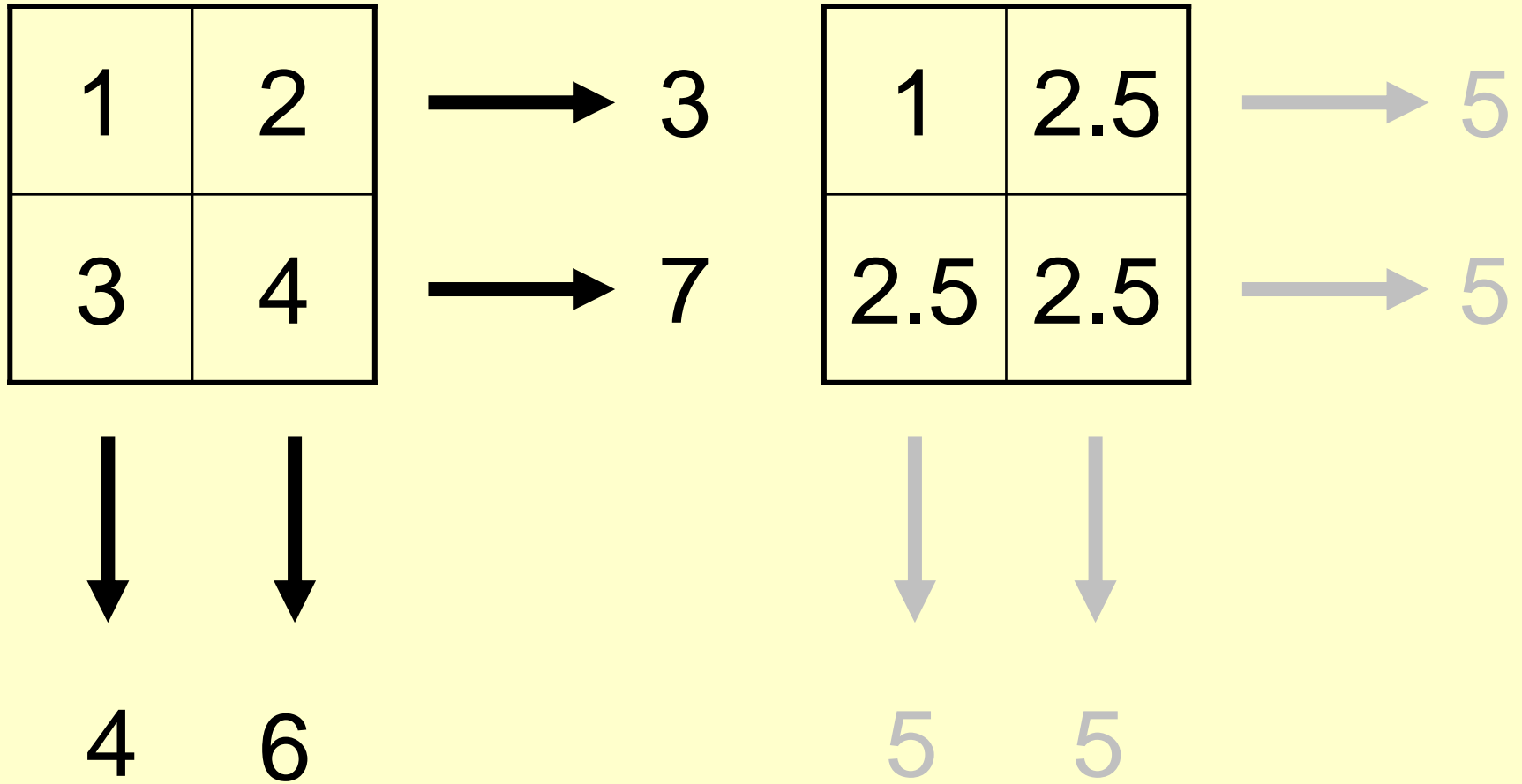
4 6



5 5

$$c_{11} = (3 - 5)/2 + (4 - 5)/2 = -2/2 - 1/2$$

$$c_{11} = -1 - 0.5 = -1.5$$



$$c_{12} = (3 - 5)/2 + (6 - 5)/2 = -2/2 + 1/2$$

$$c_{12} = -1 + 0.5 = -0.5$$

1	2
3	4

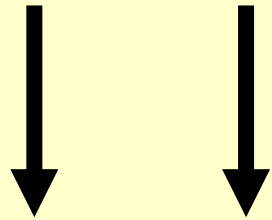
→ 3

→ 7

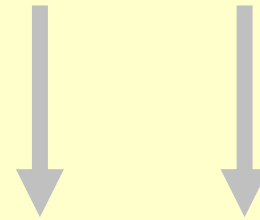
1	2
2.5	2.5

→ 5

→ 5



4 6



5 5

$$c_{13} = (7 - 5)/2 + (4 - 5)/2 = 2/2 - 1/2$$

$$c_{13} = 1 - 0.5 = 0.5$$

1	2
3	4

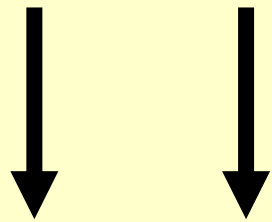
→ 3

→ 7

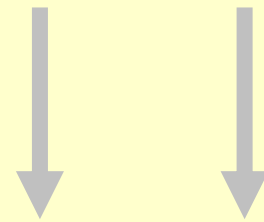
1	2
3	2.5

→ 5

→ 5



4 6



5 5

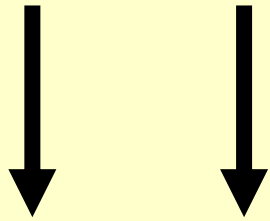
$$c_{14} = (7 - 5)/2 + (6 - 5)/2 = 2/2 + 1/2$$

$$c_{14} = 1 + 0.5 = 1.5$$

1	2
3	4

→ 3

→ 7

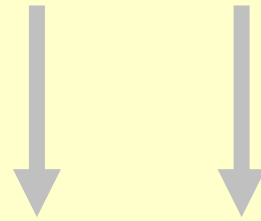


4 6

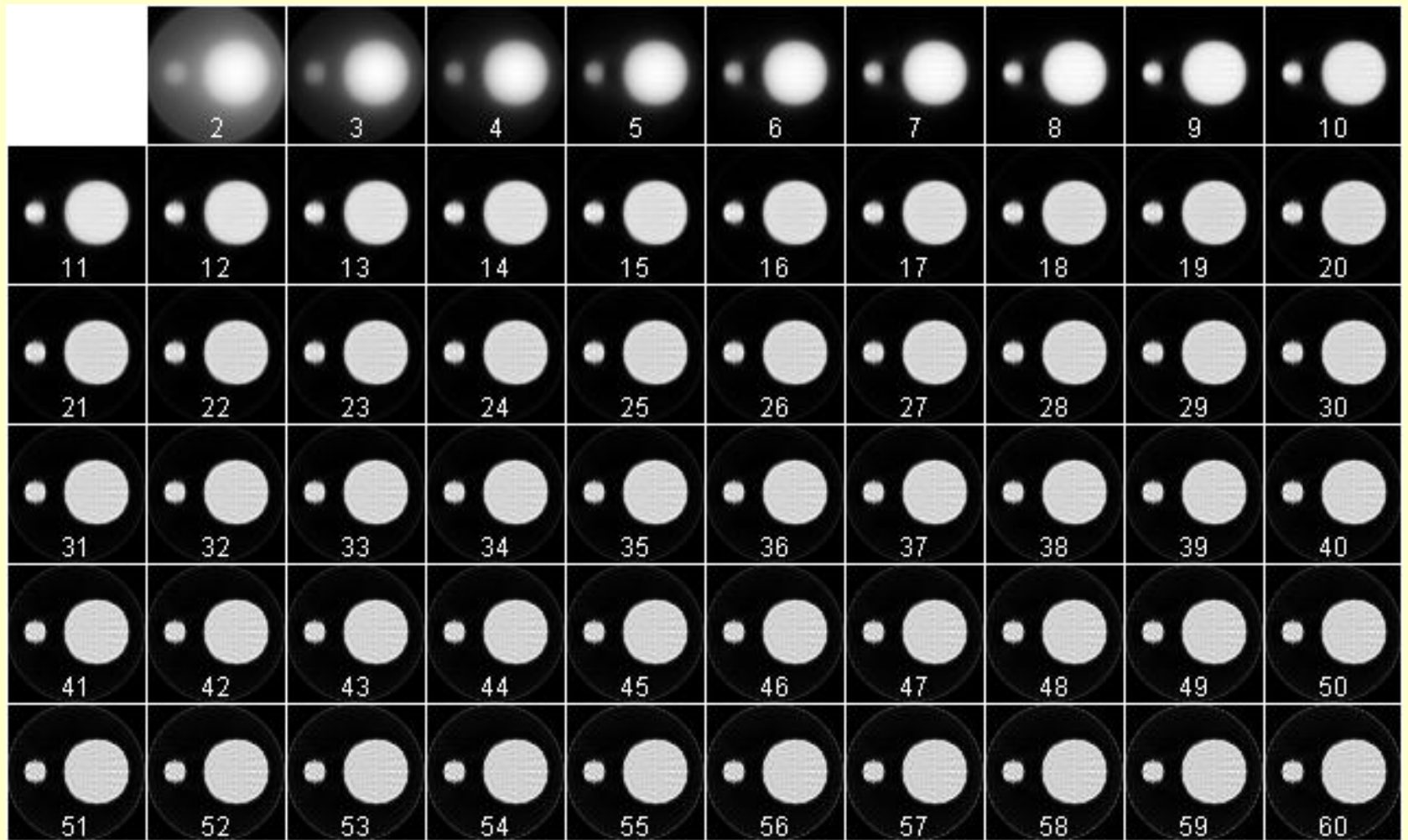
1	2
3	4

→ 5

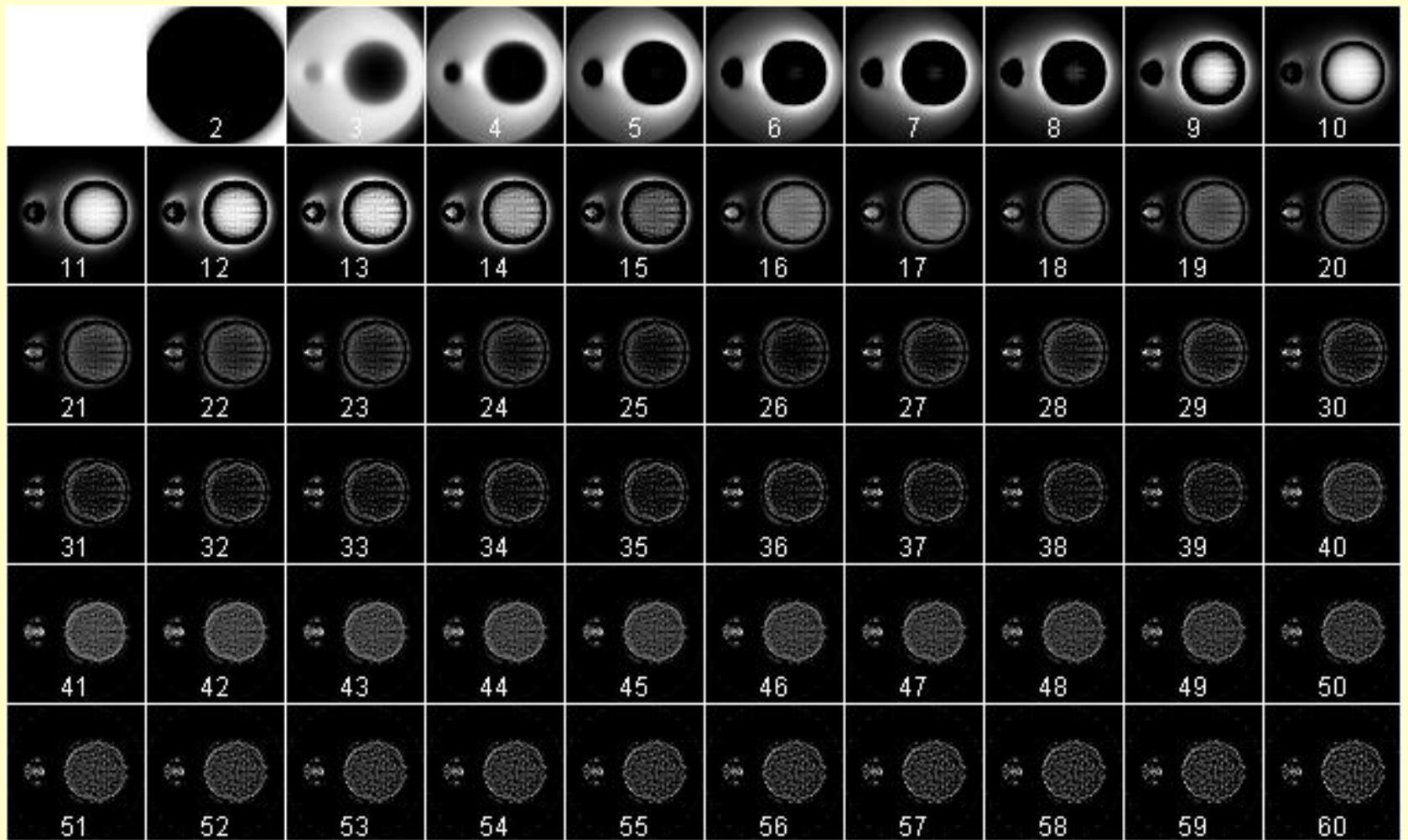
→ 5



5 5

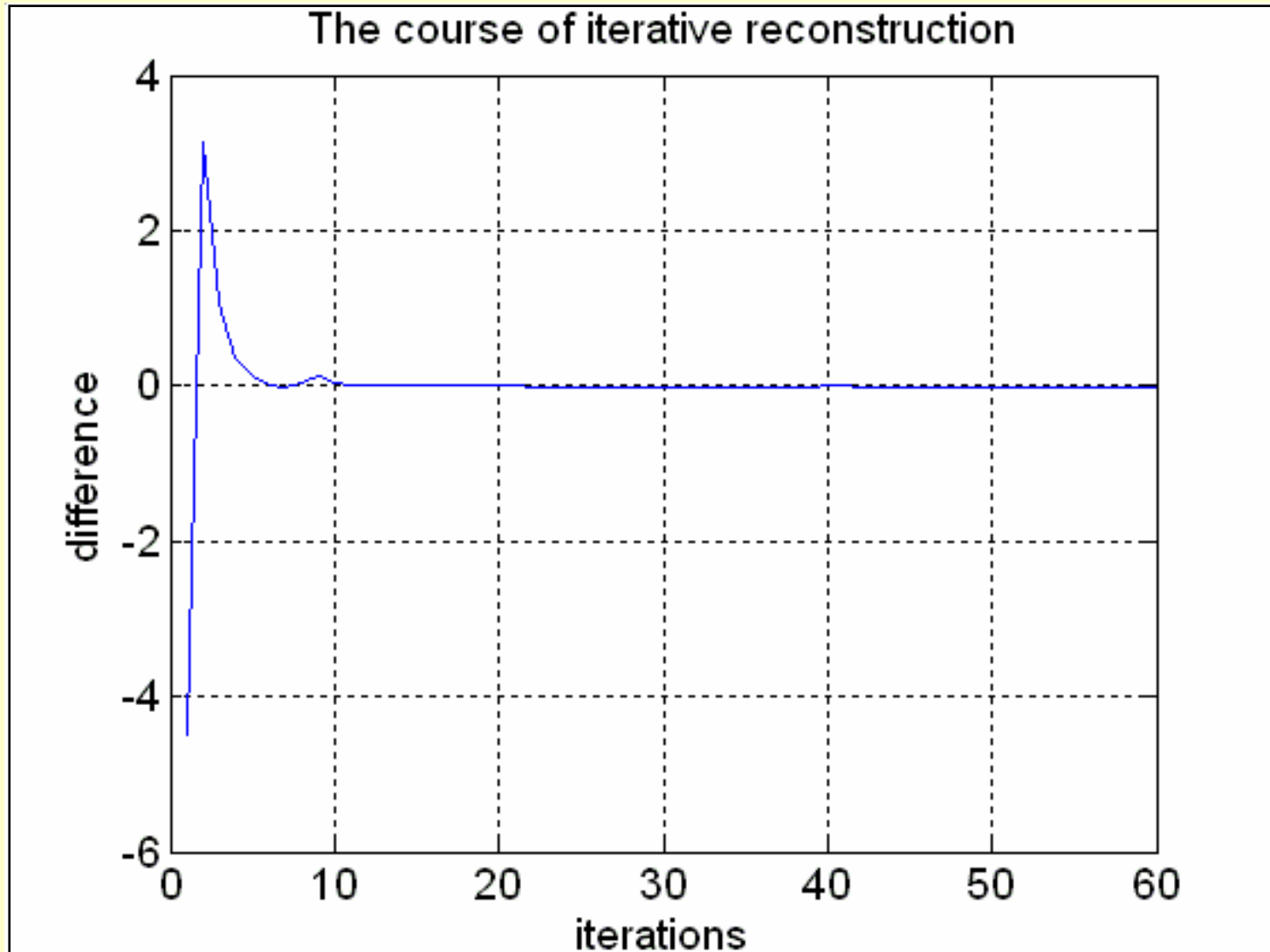


Iterative reconstruction - multiplicative corrections



Iterative reconstruction - differences between individual iterations

Iterative reconstruction - multiplicative corrections



Sequence of iterations - multiplicative corrections



estimated image



differences between
subsequent iterations

Filtered back-projection

- very fast
- direct inversion of the projection formula
- corrections for scatter, non-uniform attenuation and other physical factors are difficult
- it needs a lot of filtering - trade-off between blurring and noise
- quantitative imaging difficult

Iterative reconstruction

- discreteness of data included in the model
- it is easy to model and handle projection noise, especially when the counts are low
- it is easy to model the imaging physics such as geometry, non-uniform attenuation, scatter, etc.
- quantitative imaging possible
- amplification of noise
- long calculation time

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