# **EL582/BE620 --- Medical Imaging -**Introduction, Review of Signals & Systems, Image Quality Metrics

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Based on Prince and Links, Medical Imaging Signals and Systems and Lecture Notes by Prince. Figures are from the book.

#### **Lecture Outline**

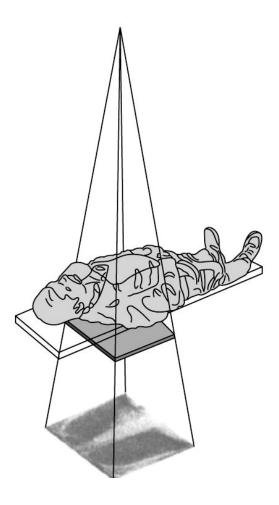
- Overview of different imaging systems
- Review of basic signals and systems
- Image quality assessment

# What is Medical Imaging?

- Using an instrument to see the inside of a human body
  - Non-invasive
  - Some with exposure to small amount of radiation (X-ray, CT and nuclear medicine)
  - Some w/o (MRI and ultrasound)
- The properties imaged vary depending on the imaging modality
  - X-ray (projection or CT): attenuation coefficient to X-ray
  - Ultrasound: sound reflectivity
  - MRI: hydrogen proton density, spin relaxation

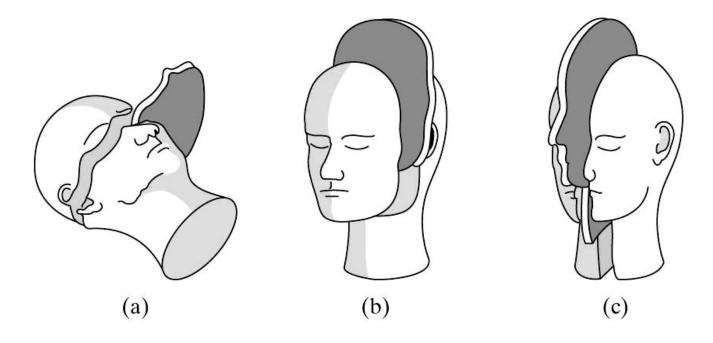
# **Projection vs. Tomography**

- Projection:
  - A single image is created for a 3D body, which is a "shadow" of the body in a particular direction (integration through the body)



# **Projection vs. Tomography**

- Tomography
  - A series of images are generated, one from each slice of a 3D object in a particular direction (axial, coronal, sagital)
  - To form image of each slice, projections along different directions are first obtained, images are then reconstructed from projections (backprojection, Radon transform)



## **Anatomical vs. Functional Imaging**

- Some modalities are very good at depicting anatomical (bone) structure
  - X-ray, X-ray CT
  - MRI
- Some modalities do not depict anatomical structures well, but reflect the functional status (blood flow, oxygenation, etc.)
  - Ultrasound
  - PET, functional MRI

Image: constrained bit with the second sec

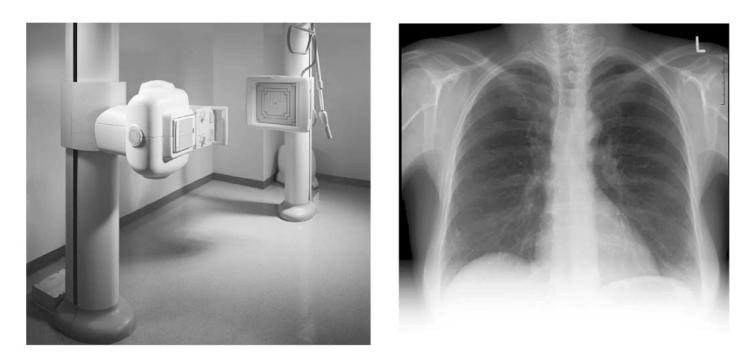
Functional

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# **Common Imaging Modalities**

- Projection radiography (X-ray)
- Computed Tomography (CT scan or CAT Scan)
- Nuclear Medicine (SPECT, PET)
- Ultrasound imaging
- MRI

#### **Projection Radiography**

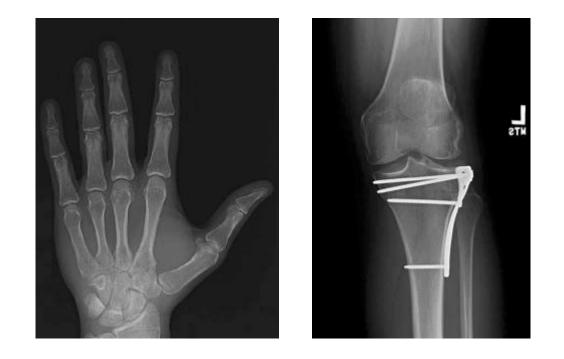


(a)

(b)



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- Year discovered:
- Form of radiation: radiation
- Energy / wavelength of radiation:
- Imaging principle:
- Imaging volume:
- Resolution:
- Applications:

1895 (Röntgen, NP 1905) X-rays = electromagnetic (photons) 0.1 - 100 keV / 10 - 0.01 nm (ionizing) X-rays penetrate tissue and create "shadowgram" of differences in density. Whole body Very high (sub-mm) Mammography, lung diseases, orthopedics, dentistry, cardiovascular, GI

From Graber, Lecture Note for Biomedical Imaging, SUNY

#### **Computed Tomography**





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- Year discovered:
- Form of radiation:
- Energy / wavelength of radiation:
- Imaging principle:

views are

- Imaging volume:
- Resolution:
- Applications:

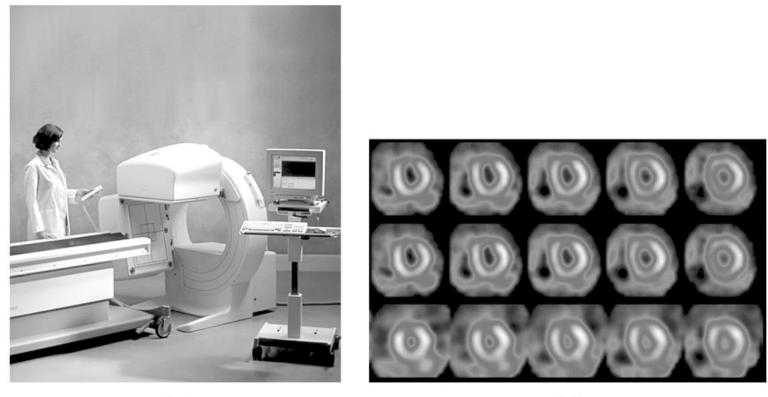
1972 (Hounsfield, NP 1979) X-rays 10 – 100 keV / 0.1 – 0.01 nm (ionizing) X-ray images are taken under many angles from which tomographic ("sliced") computed Whole body High (mm) Soft tissue imaging (brain, cardiovascular, GI)

From Graber, Lecture Note for Biomedical Imaging, SUNY

## **Nuclear Medicine**

- Images can only be made when appropriate radioactive substances (called radiotracer) are introduced into the body that emit gamma rays.
- A nuclear medicine image reflects the local concentration of a radiotracer within the body
- Three types
  - Conventional radionuclide imaging or scintigraphy
  - Single photon emission computed tomography (SPECT)
  - Positron emission tomography (PET)

#### SPECT



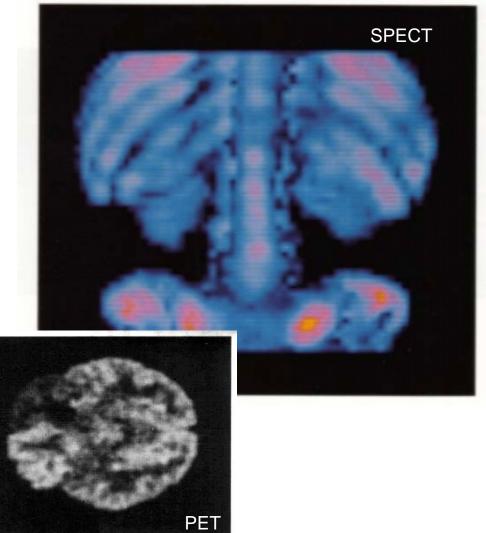
(a)

(b)

Figure 1.3

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• What do you see?

- Year discovered:
- Form of radiation:
- Energy / wavelength of radiation:
- Imaging principle:

body cameras.

- Imaging volume:
- Resolution:
- Applications:

processes,

1953 (PET), 1963 (SPECT) Gamma rays > 100 keV / < 0.01 nm (ionizing) Accumulation or "washout" of radioactive isotopes in the are imaged with x-ray

Whole body Medium – Low (mm - cm) Functional imaging (cancer detection, metabolic myocardial infarction)

From Graber, Lecture Note for Biomedical Imaging, SUNY

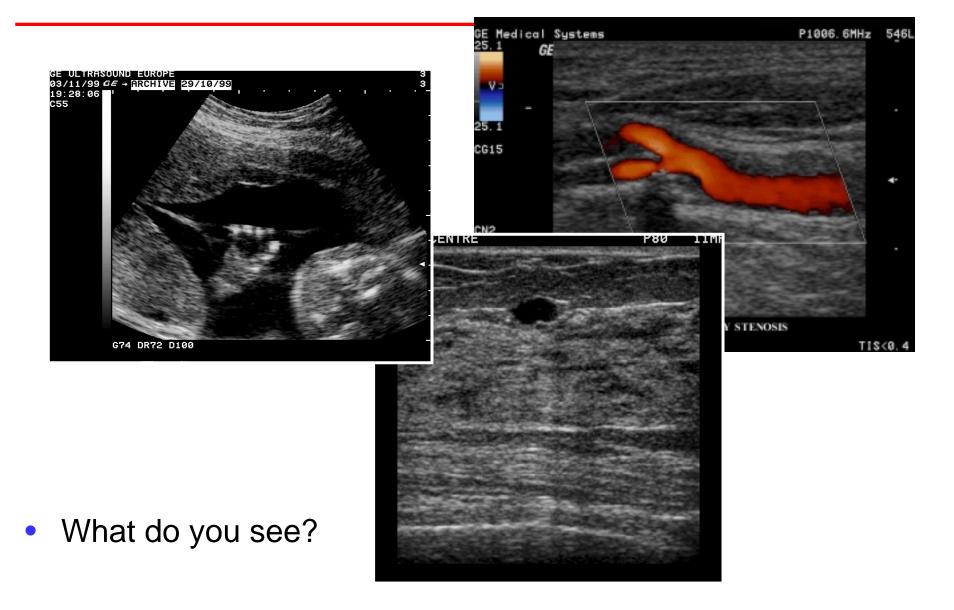
# **Ultrasound Imaging**

- High frequency sound are emitted into the imaged body, time of return of these sound pulses are measured
- Comparatively inexpensive and completely non-invasive
- Image quality is relatively poor





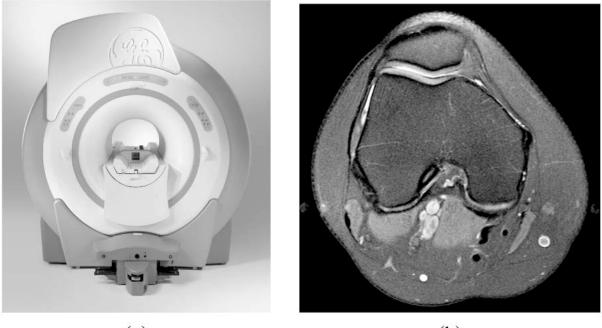
(b)



•	Year discovered:	1952 (clinical: 1962)
•	Form of radiation:	Sound waves (non-ionizing) <b>NOT</b> EM radiation!
•	Frequency / wavelength of radiation:	1 – 10 MHz / 1 – 0.1 mm
•	Imaging principle:	Echoes from discontinuities in tissue density/speed of sound
	are	registered.
•	Imaging volume:	< 20 cm
•	Resolution:	High (mm)
•	Applications: (Doppler)	Soft tissue, blood flow

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#### **Magnetic Resonance Imaging**



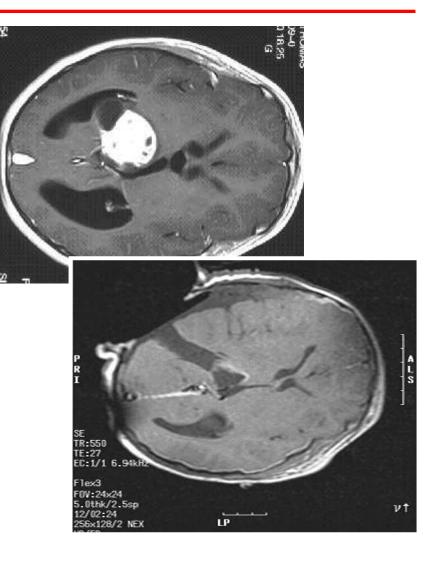






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• What do you see?

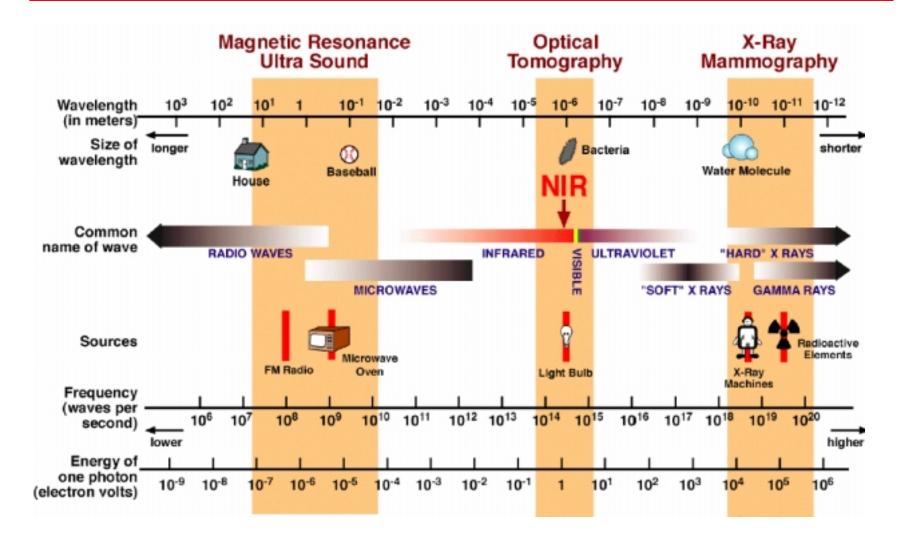
• Year discovered:

- Form of radiation:
- Energy / wavelength of radiation:
- Imaging principle: and response
- Imaging volume:
- Resolution:
- Applications:

1945 ([NMR] Bloch, NP 1952) 1973 (Lauterbur, NP 2003) 1977 (Mansfield, NP 2003) 1971 (Damadian, SUNY DMS) Radio frequency (RF) (non-ionizing) 10 – 100 MHz / 30 – 3 m (~10-7 eV) Proton spin flips are induced, the RF emitted by their (echo) is detected. Whole body High (mm) Soft tissue, functional imaging

From Graber, Lecture Note for Biomedical Imaging, SUNY

#### **Waves Used by Different Modalities**



### **Course breakdown**

- Biomedical Imaging is a multi-disciplinary field involving
  - Physics (matter, energy, radiation, etc.)
  - Math (linear algebra, calculus, statistics)
  - Biology/Physiology
  - Engineering (implementation)
  - Image processing (image reconstruction and enhancement and analysis)
- Course breakdown:
  - 1/3 physics
  - 1/3 instrumentation
  - 1/3 signal processing
- Understand the imaging system from a "signals and systems" point of view

#### **Signals and Systems View Point**

- The object being imaged is an input signal
  - Typically a 3D signal
- The imaging system is a transformation of the input signal to an output signal
- The image produced is an output signal
  - Typically a 2D signal (an image, e.g. an X-ray) or a series of 2D signals (e.g. images from a CT scan)

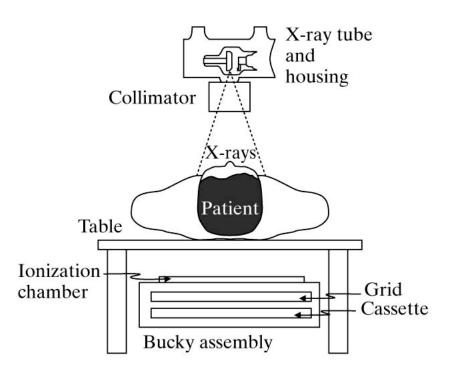
input signal  $\rightarrow$  system or process  $\rightarrow$  output signal

# **Example: Projection X-Ray**

- Input signal: μ(x; y) is the linear attenuation coefficient for x-rays of a body component along a line
- Imaging Process: integration over *x* variable:

 $g(y)=\int \mu(x,y)dx$ 

• Output signal: g(y)





# **Example Signals**

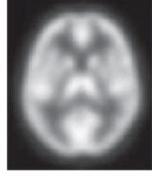
- $\mu(x, y, z)$ , linear attenuation coefficient in xrays
- h(x, y, z), <u>CT numbers</u> in computed tomography
- A(x, y, z), <u>radioactivity</u> in nuclear medicine







subdura hemotoma pushing midline R to L



Positron Emission Tomography

# **Transformation of Signals**

- Components of a transformation:
  - Input: f
  - System:  $\mathcal{H}[\cdot]$
  - Output: g
- The <u>impulse response</u> or <u>point spread function</u> due to an impulse at  $(\xi, \eta)$  is

$$h(x, y; \xi, \eta) = \mathcal{H}[\delta(x - \xi, y - \eta)]$$

## **Linear Systems**

• A <u>linear system</u> satisfies:

 $\mathcal{H}[w_1f_1 + w_2f_2] = w_1\mathcal{H}[f_1] + w_2\mathcal{H}[f_2]$ 

for all signals  $f_1$  and  $f_2$  and weights  $w_1$  and  $w_2$ .

• A linear system satisfies the <u>superposition</u> <u>integral</u>

$$g(x,y) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} h(x,y;\xi,\eta) f(\xi,\eta) d\xi d\eta$$

• We model most medical imaging systems as linear.

## **Shift-Invariant Systems**

• A system is  $\underline{\text{shift-invariant}}$  is

$$g(x - x_0, y - y_0) = \mathcal{H}[f(x - x_0, y - y_0)]$$
  
for every  $(x_0, y_0)$  and  $f(\cdot, \cdot)$ .  
• A linear shift-invariant (LSI) system yields  
 $h(x, y; \xi, \eta) \rightarrow h(x - \xi, y - \eta)$   
[Watch out for abuse of notation]

## **Linear and Shift-Invariant System**

• An LSI system satisfies the <u>convolution integral</u>

$$g(x,y)=\int_{-\infty}^{\infty}\!\!\int_{-\infty}^{\infty}h(x\!-\!\xi,y\!-\!\eta)f(\xi,\eta)d\xi d\eta$$

which is abbreviated as

$$g(x,y) = h(x,y) \ast f(x,y)$$

 We model most medical imaging systems as LSI

h(x,y) is called the Impulse Response or Point Spread Function (PSF) of a LSI system, which indicates the output signal corresponding to a single impulse or point at origin.

## Fourier Transform: 1D signals

$$\begin{array}{lll} F(u) &=& \int_{-\infty}^{\infty} f(x) e^{-j2\pi u x} dx \\ f(x) &=& \int_{-\infty}^{\infty} F(u) e^{+j2\pi u x} du \end{array}$$

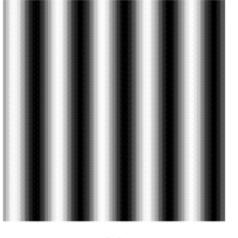
- *x* has units of length (mm, cm, m) or time (for 1D signal in time)
- *u* has units of inverse length (cycles/unit-length), which is referred to as spatial frequency, or inverse time (cycles/sec), which is referred to as temporal frequency
- /F(u)/ indicts the amount of signal component in f(x) with frequency u

### Fourier Transform: 2D signals

$$\begin{split} F(u,v) &= \mathcal{F}\{f\} \\ &= \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(x,y) e^{-j2\pi(ux+vy)} dx dy \\ f(x,y) &= \mathcal{F}^{-1}\{F\} \\ &= \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} F(u,v) e^{+j2\pi(ux+vy)} du dv \end{split}$$

- 2D signal's frequency can be measured in different directions (horizontal, vertical, 45<sup>^</sup>, etc.), but only two orthogonal directions are necessary
- *u* and *v* indicate cycles/horizontal-unit and cycles/vertical-unit
- |F(u,v)| indicates the amount of signal component with frequency u,v.

#### **Spatial Frequency**



(a)

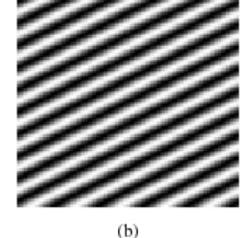


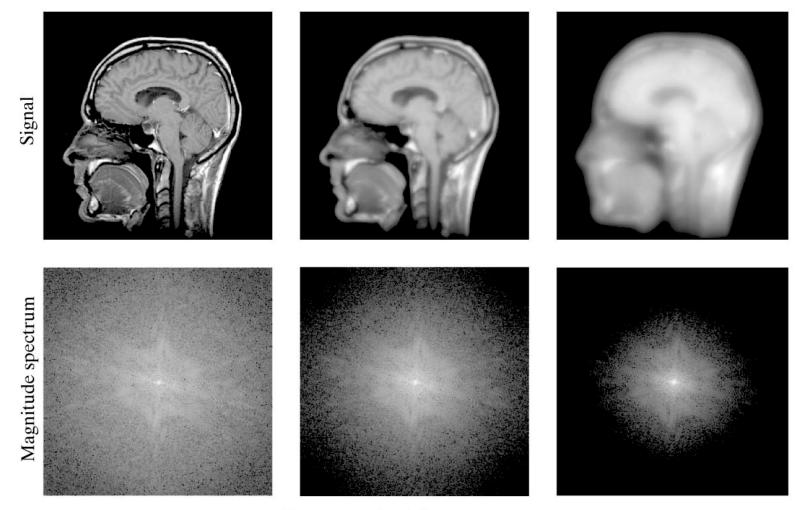
Figure 2.1 Two-dimensional sinusoidal signals: (a)  $(f_x, f_y) = (5, 0)$ ; (b)  $(f_x, f_y) = (5, 10)$ . The horizontal and vertical units are the width and height of the image, respectively. Therefore,  $f_x = 5$  means that there are five cycles along each row.

## **Spatial Frequency**

- Spatial frequency measures how fast the image intensity changes in the image plane
- Spatial frequency can be completely characterized by the variation frequencies in two orthogonal directions (e.g horizontal and vertical)
  - $f_x$ : cycles/horizontal unit distance
  - $f_{y}$ : cycles/vertical unit distance
- It can also be specified by magnitude and angle of change

$$f_m = \sqrt{f_x^2 + f_y^2}, \theta = \arctan(f_y / f_x)$$

# **FT of Typical Images**



Decreasing high-frequency content

#### Convolution Property and Frequency Response

• Convolution in space domain = Product in frequency domain

$$\mathcal{F}\{f_1 * f_2\} = F_1 F_2$$

• For LSI system

Impulse response

$$G(x,y) = h(x,y) * f(x,y)$$
  

$$G(u,v) = H(u,v) F(u,v)$$
  
Frequency response

H(u,v) indicates how a complex exponential signal with frequency u,v will be modified by the system in its magnitude and phase

 $\checkmark$ 

$$e^{-j2\pi(ux+vy)} \to H(u,v)e^{-j2\pi(ux+vy)} = |H(u,v)|e^{-j(2\pi(ux+vy)+\angle H(u,v))}$$

## **Extra Readings**

- See Chap 2 of textbook for more extensive reviews of signals and systems
- For more exposition, see
  - Oppenheim and Wilsky, Signals and Systems
- We will review a particular subject more when needed

## **Image Quality**

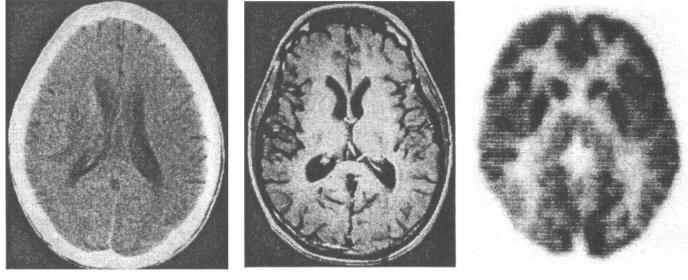
- Introduction
- Contrast
- Resolution
- Noise
- Artifacts
- Distortions

## **Measures of Quality**

- Physics-oriented issues:
  - contrast, resolution
  - noise, artifacts, distortion
  - Quantitative accuracy
- Task-oriented issues:
  - sensitivity, specificity
  - diagnostic accuracy

## What is Contrast?

- Difference between image characteristics of an object of interest and surrounding objects or background
- Which image below has higher contrast?





(b)

(c)

Figure I.4

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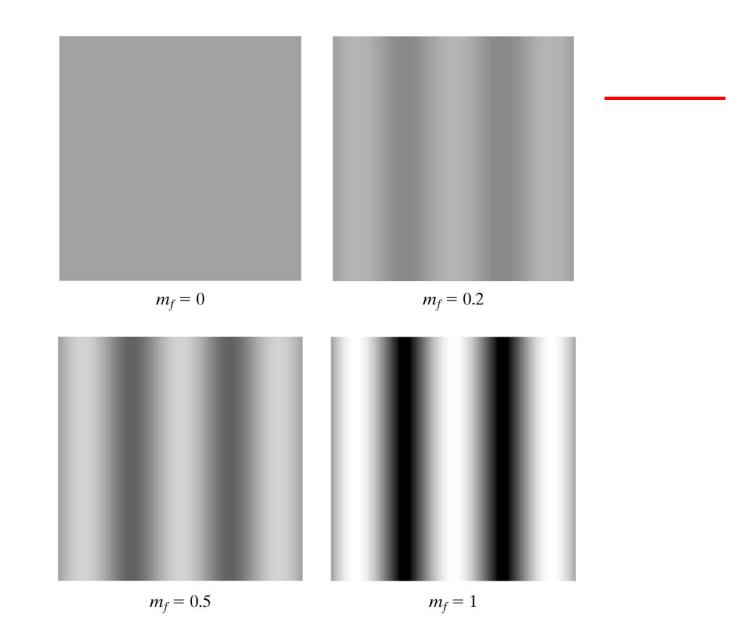
## Contrast

- Contrast: Difference between image characteristics of an object of interest and surrounding objects or background
- General definition
  - $f_{\text{max}},\,f_{\text{min}}$ : maximum and minimum values of the signal in an image

 $\underline{\text{Contrast}} = \underline{\text{modulation}} =$  $m_f = \frac{\text{amplitude}}{\text{average}} = \frac{f_{\text{max}} - f_{\text{min}}}{f_{\text{max}} + f_{\text{min}}}$ 

• For a sinusoidal signal

$$f(x,y) = A + B\sin(2\pi u_0 x) \qquad \qquad m_f = \frac{B}{A}$$





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## **Modulation Transfer Function**

• The actual signal being imaged can be decomposed into many sinusoidal signals with different frequencies

$$f(x, y) = A + \sum_{k} B_{k} \sin(2\pi u_{k} x + 2\pi v_{k} y); \quad m_{f,k} = \frac{B_{k}}{A}$$

- Suppose the imaging system can be considered as a LSI system with frequency response H(u,v)
- Imaged signal is

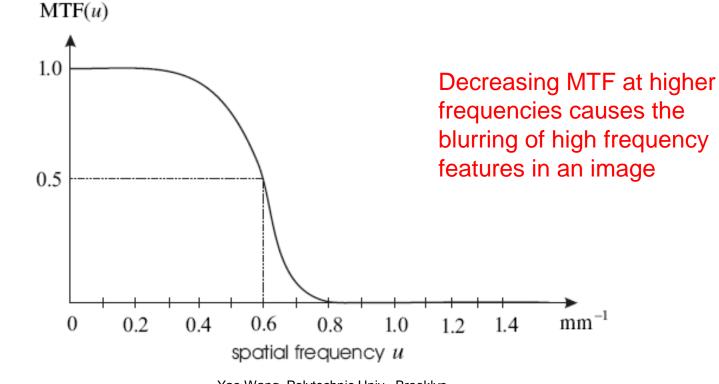
$$g(x, y) = H(0,0)A + \sum_{k} H(u_{k}, v_{k})B_{k} \sin(2\pi u_{k}x + 2\pi v_{k}y); \quad m_{g,k} = \frac{|H(u_{k}, v_{k})|B_{k}}{H(0,0)A}$$

 The MTF refers to the ratio of the contrast (or modulation) of the imaged signal to the contrast of the original signal at different frequencies

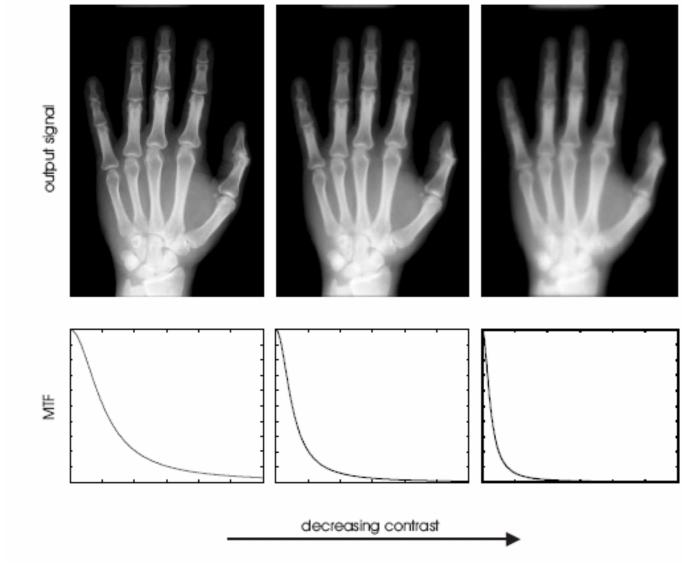
$$MTF(u,v) = \frac{m_{g,u,v}}{m_{f,u,v}} = \frac{|H(u,v)|}{H(0,0)}$$

## **More on MTF**

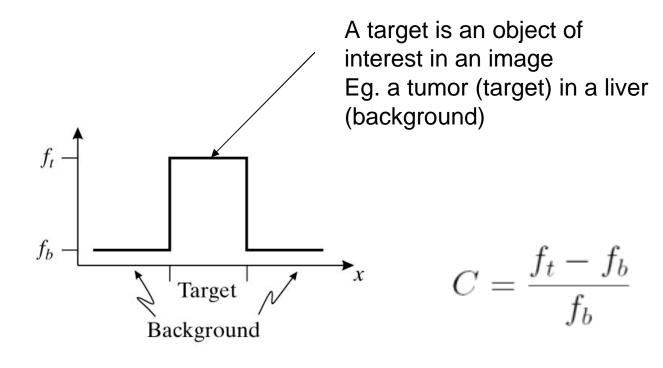
- MTF characterizes how the contrast (or modulation) of a signal component at a particular frequency changes after imaging
- MTF = magnitude of the frequency response of the imaging system (normalized by H(0,0))
- Typically  $0 \le MTF(u, v) \le MTF(0, 0) = 1$

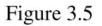


#### Impact of the MTF on the Image Contrast



### **Local Contrast**

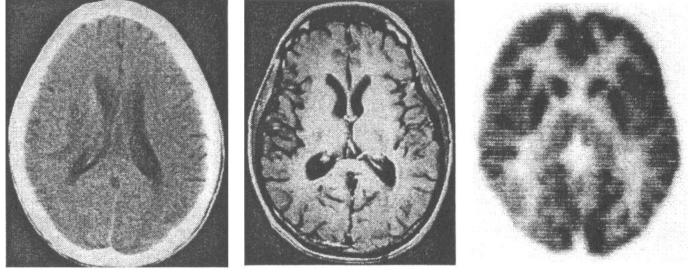




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## What is Resolution?

- The ability of a system to depict spatial details.
- Which image below has higher resolution?





(b)

(c)

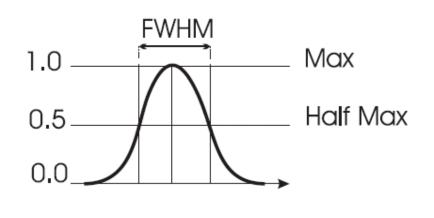
Figure I.4

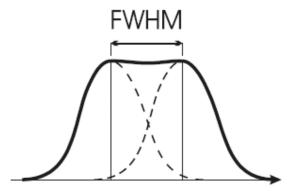
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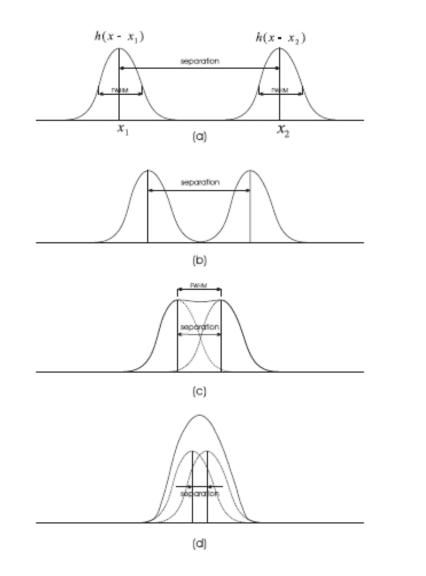
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# Resolution

- Resolution refers to the ability of a system to depict spatial details.
- Resolution of a system can be characterized by its line spread function
  - How wide a very thin line becomes after imaging
  - Full width at half maximum (FWHM) determines the distance between two lines which can be separated after imaging
  - The smaller is FWHM, the higher is the resolution







Distance > FWHM

Distance > FWHM

Distance = FWHM (barely separate)

Distance < FWHM (cannot separate)

## **Resolution and MTF**

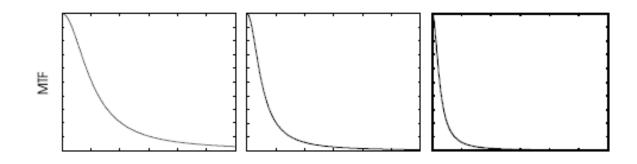
- A pure vertical sinusoidal pattern can be thought of as the blurred image of uniformly spaced vertical lines
- The distance between lines is equal to distance between maxima
- If the frequency =  $u_0$ , the distance =  $1/u_0$

 $f(x, y) = A + B\sin(2\pi u_0 x)$   $g(x, y) = H(0,0)A + H(u_0,0)\sin(2\pi u_0 x)$  $= H(0,0)A + MTF(u_0,0)H(0,0)\sin(2\pi u_0 x)$ 

- If MTF(u<sub>0</sub>)=0, the sinusoidal patterns become all constant and one cannot see different lines
- If MTF(u) first becomes 0 at frequency  $u_{c_{,}}$  the minimum distance between distinguishable lines = 1/  $u_{c}$
- Resolution is directly proportional to the stopband edge in MTF

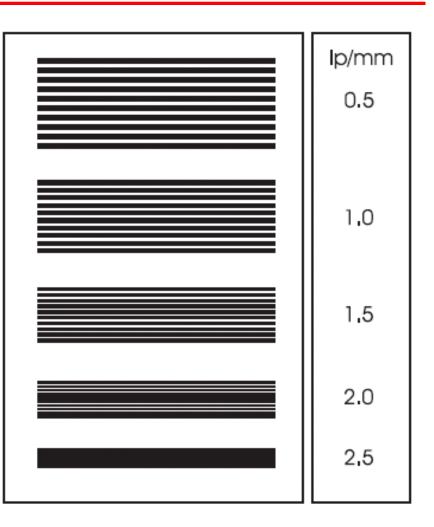
## Example

• Which system below has better contrast and resolution?



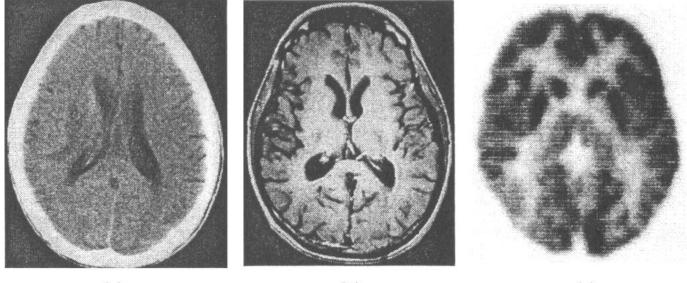
## **Bar Phantom**

- The resolution of an imaging system can be evaluated by imaging a bar phantom.
- The resolution is the frequency (in lp/mm) of the finest line group that can be resolved after imaging.
  - Gamma camera: 2-3 lp/cm
  - CT: 2 lp/mm
  - chest x-ray: 6-8 lp/mm



## What is noise?

- Random fluctuations in image intensity that are not due to actual signal
- The source of noise in an imaging system depends on the physics and instrumentation of the imaging modality
- Which image below is most noisy?





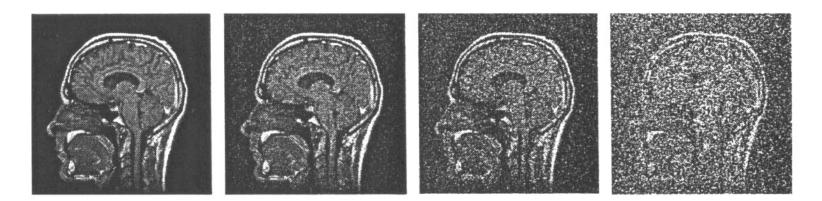


(c)

Figure I.4

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#### Noise



Increasing noise

Figure 3.10

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## White vs. Correlated Noise

Model of a typical imaging system

$$g(x,y) = f(x,y) * h(x,y) + N(x,y)$$

N(x, y) is noise N(x, y) is a <u>random variable</u> at each (x, y)N(x, y) could be <u>continuous</u> or <u>discrete</u>

- White Noise: Noise values at different positions are independent of each other
  - Mean and variance at different (x,y) are same
- Correlated noise: noise at adjacent positions are correlated
  - Described by the correlation function R(x,y), whose Fourier transform is the noise power spectrum (NPS) NPS(u,v)
  - White noise has a PSD = constant = variance

## **Random Variables**

- The most complete description of a random variable is its probability density function (pdf) for continuous-valued RV, or probability mass function (pmf) for discrete-valued RV.
- The two most important statistics of a random variable is mean (μ) and standard deviation (σ). The power of a random signal = variance = σ<sup>2</sup>. Both η and σ can be derived from the pdf or pmf of a RV.
- Noise typically has zero mean ( $\eta=0$ ).

# **Amplitude Signal to Noise Ratio**

Amplitude SNR

$$\mathrm{SNR}_a = \frac{\mathrm{amplitude}(f)}{\mathrm{amplitude}(N)}$$

- Meaning of "signal amplitude" and "noise amplitude" are casedependent.
- For projection radiography, the number of photons G counted per unit area follows a Poisson distribution. The signal amplitude is the average photon number per unit area ( $\mu$ ) and the noise amplitude is the standard deviation of G

$$SNR_a = \frac{\mu_G}{\sigma_G} = \frac{\mu}{\sqrt{\mu}} = \sqrt{\mu}$$

A higher exposure can lead to higher SNR<sub>a</sub>

## **Power SNR**

- Power SNR  $\mathrm{SNR}_p = \frac{\mathrm{power}(f)}{\mathrm{power}(N)}$
- Signal power:

$$power(f) = \iint_{x,y} |h(x, y)|^{2} f(x, y)|^{2} dx dy = \iint_{u,v} |H(u, v)F(u, v)|^{2} du dv$$

Approximation:  $power(f) = A^2$ , A is the average value of the signal Approximation:  $power(f) = \sigma_f^2$ , variance of the signal

- Noise power:  $power(N) = \iint_{u,v} NPS(u,v) dudv$
- For white noise:  $power(N) = \sigma_N^2$

# SNR in dB

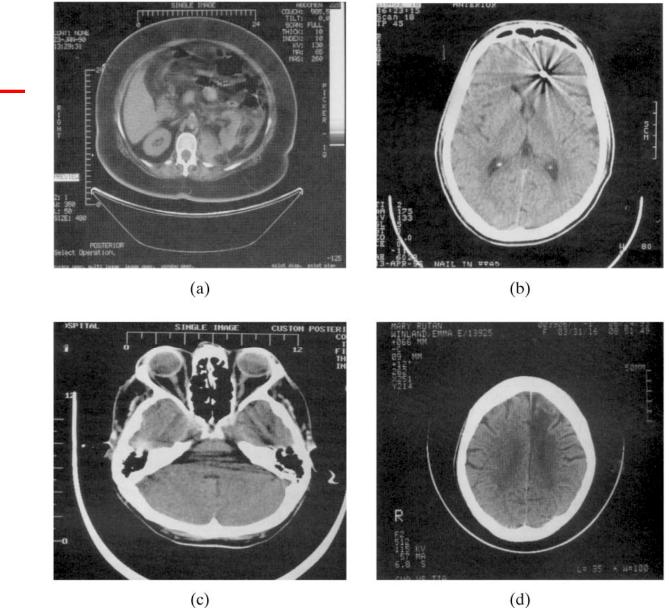
- SNR is more often specified in decibels (dB)
- SNR in dB
  - SNR (dB) = 20 log  $_{10}$  SNR $_{a}$ 
    - $= 10 \log_{10} SNR_{p}$
- Example:
  - SNR<sub>p</sub>=2, SNR (dB)=3 dB
  - SNR<sub>p</sub>=10, SNR (dB)=10 dB
  - SNR<sub>p</sub>=100, SNR (dB)=20 dB

## Artifacts, distortion & accuracy

- Artifacts:
  - Some imaging systems can create image features that do not represent a valid object in the imaged patient, or false shapes/textures.
- Distortion
  - Some imaging system may distort the actual shape/position and other geometrics of imaged object.
- Accuracy
  - Conformity to truth and clinical utility

## **Non-Random Artifacts**

- Artifacts: image features that do not correspond to a real object, and are not due to noise
  - Motion artifacts: blurring or streaks due to patient motion
  - star artifact: in CT, due to presence of metallic material in a patient
  - beam hardening artifact: broad dark bands or streaks, due to significant beam attenuation caused by certain materials
  - ring artifact: because detectors are out of calibration



Star artifact

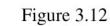
Ring

artifact

Beam hardening

Motion

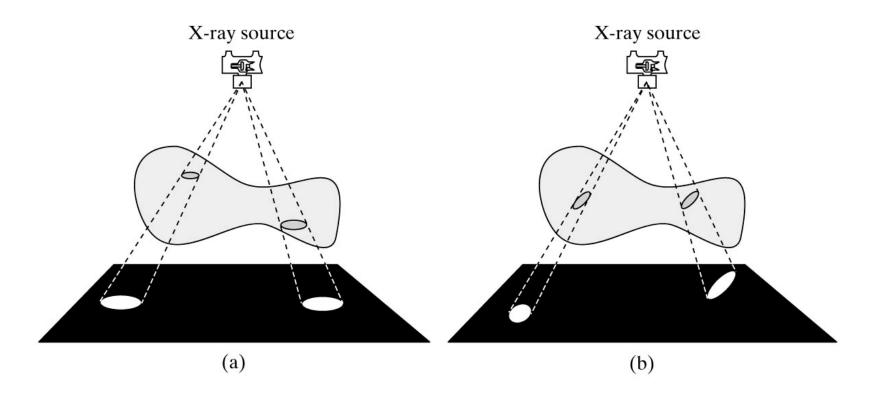
artifact

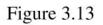


EL582, Intro

Medical Imaging Signals and Systems, by Jerry L. Prince and Jonathan Links. ISBN 0-13-065353-5. © 2006 Pearson Education, Inc., Upper Saddle River, NJ. All rights reserved.

## **Geometric Distortion**





*Medical Imaging Signals and Systems*, by Jerry L. Prince and Jonathan Links. ISBN 0-13-065353-5. © 2006 Pearson Education, Inc., Upper Saddle River, NJ. All rights reserved.

- In (a): two objects with different sizes appear to have the same size
- In (b): two objects with same shape appear to have different shapes

### Accuracy

- Accuracy:
  - conformity to truth
    - quantitative accuracy
  - clinical utility
    - diagnostic accuracy
- Quantitative accuracy:
  - numerical accuracy: accuracy in terms of signal value
    - bias (systematic, e.g. due to miscalibration), imprecision (random)
  - geometric accuracy: accuracy in terms of object size/shape

## **Diagnostic Accuracy**

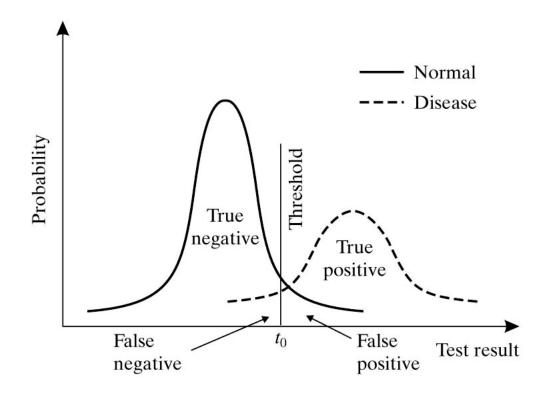
#### • Contingency Table

		Disease	
		+	١
Test	+	а	b
	-	С	d

a = # w/disease & test says disease b = # w/o disease & test says disease c = # w/disease & test says normald = # w/o disease & test says normal

sensitivity = 
$$\frac{a}{a+c}$$
  
specificity =  $\frac{d}{b+d}$   
diagnostic accuracy =  $\frac{a+d}{a+b+c+d}$ 

 If the diagnosis is based on a single value of a test result and the decision is based on a chosen threshold, the sensitivity and specificity can be visualized as follows



### Reference

 Prince and Links, Medical Imaging Signals and Systems, Chap 1-3.

## Homework

- Reading:
  - Prince and Links, Medical Imaging Signals and Systems, Chap 1-3.
- Note down all the corrections for Ch. 1-3 on your copy of the textbook based on the provided errata.
- Problems for Chap 3 of the text book:
  - P3.2
  - P3.5
  - P3.7
  - P3.9
  - P3.11
  - P3.16
  - P3.22 (note correction in the Errata)