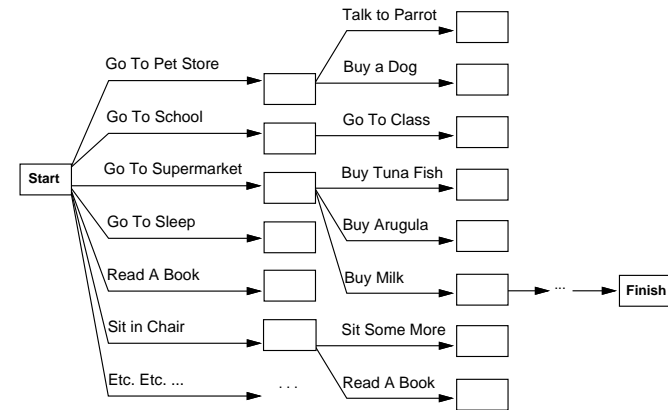


# PLANNING

## CHAPTER 10

### Search vs. planning

Consider the task *get milk, bananas, and a cordless drill*  
 Standard search algorithms seem to fail miserably:



After-the-fact heuristic/goal test inadequate

### Outline

- ◇ Search vs. planning
- ◇ STRIPS operators
- ◇ Partial-order planning

### Search vs. planning contd.

Planning systems do the following:

- 1) open up action and goal representation to allow selection
- 2) divide-and-conquer by subgoaling
- 3) relax requirement for sequential construction of solutions

	Search	Planning
<b>States</b>	Lisp data structures	Logical sentences
<b>Actions</b>	Lisp code	Preconditions/outcomes
<b>Goal</b>	Lisp code	Logical sentence (conjunction)
<b>Plan</b>	Sequence from $S_0$	Constraints on actions

## STRIPS operators

Tidily arranged actions descriptions, restricted language

ACTION:  $Buy(x)$

PRECONDITION:  $At(p), Sells(p, x)$

EFFECT:  $Have(x)$

$At(p) Sells(p, x)$

**Buy(x)**

$Have(x)$

[Note: this abstracts away many important details!]

Restricted language  $\Rightarrow$  efficient algorithm

- Precondition: conjunction of positive literals
- Effect: conjunction of literals
  - positive effect: add literals
  - negative effect: remove literals (negated literals)

## Forward State-space Search

◇ aka Progression Planning

◇ similar to Forward Chaining

◇ State-space formulation

- Initial State: initial KB
- Actions: operators whose preconditions are satisfied
  - successors:
    - \* positive effect: add literals
    - \* negative effect: remove literals
- Goal test: goal state
- Step cost: typically 1

## Backward State-space Search

◇ aka Regression Planning

◇ similar to Backward Chaining

◇ Difficult if the goal is described as constraints (e.g. 4 gallons in the large jug)—potentially many goal states.

◇ A goal can be divided into sub-goals (children).

◇ State-space formulation

- Initial State: goal state
- Actions: operations that can achieve the goal/sub-goal
  - not undo any super-goals [parent goals/preconditions]
  - successors:
    - \* sub-goals (unsatisfied preconditions)
- Goal test: no sub-goals (no unsatisfied preconditions)

## Admissible Heuristics

◇ Relaxed problem

- remove all preconditions—every action is applicable
- remove all negative effects—no action removes a literal (note that the goal is a conjunction of literals)
- subgoal independence—achieving one subgoal does not affect achieving another subgoal

## Keeping track of change—Situation Calculus

Facts hold in **situations**, rather than eternally

E.g.,  $Holding(Gold, Now)$  rather than just  $Holding(Gold)$

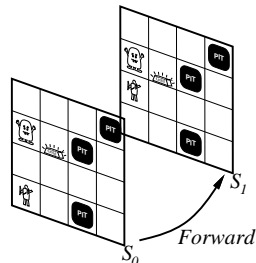
**Situation calculus** is one way to represent change in FOL:

Adds a situation argument to each non-eternal predicate

E.g.,  $Now$  in  $Holding(Gold, Now)$  denotes a situation

Situations are connected by the **Result** function

$Result(a, s)$  is the situation that results from doing  $a$  in  $s$



## Describing actions I

“Effect” axiom—describe changes due to action

$\forall s \ AtGold(s) \Rightarrow Holding(Gold, Result(Grab, s))$

“Frame” axiom—describe **non-changes** due to action

$\forall s \ HaveArrow(s) \Rightarrow HaveArrow(Result(Grab, s))$

**Frame problem**: find an elegant way to handle non-change

(a) representation—avoid frame axioms

(b) inference—avoid repeated “copy-overs” to keep track of state

**Qualification problem**: true descriptions of real actions require endless caveats—what if gold is slippery or nailed down or ...

**Ramification problem**: real actions have many secondary consequences—what about the dust on the gold, wear and tear on gloves, ...

## Describing actions II

**Successor-state axioms** solve the representational frame problem

Each axiom is “about” a **predicate** (not an action per se):

$P$  true afterwards  $\Leftrightarrow$  [an action made  $P$  true  
 $\vee$   $P$  true already and no action made  $P$  false]

For holding the gold:

$\forall a, s \ Holding(Gold, Result(a, s)) \Leftrightarrow$   
 $[(a = Grab \wedge AtGold(s)) \vee (Holding(Gold, s) \wedge a \neq Release)]$

## Making Plans

Initial condition in KB:

$At(Agent, [1, 1], S_0)$

$At(Gold, [1, 2], S_0)$

Query:  $Ask(KB, \exists s \ Holding(Gold, s))$

i.e., in what situation will I be holding the gold?

Answer:  $\{s / Result(Grab, Result(Forward, S_0))\}$

i.e., go forward and then grab the gold

This assumes that the agent is interested in plans starting at  $S_0$  and that  $S_0$  is the only situation described in the KB

## Making plans: A better way

Represent plans as action sequences  $[a_1, a_2, \dots, a_n]$

$PlanResult(p, s)$  is the result of executing  $p$  in  $s$

Then the query  $Ask(KB, \exists p \text{ Holding}(Gold, PlanResult(p, S_0)))$   
has the solution  $\{p/[Forward, Grab]\}$

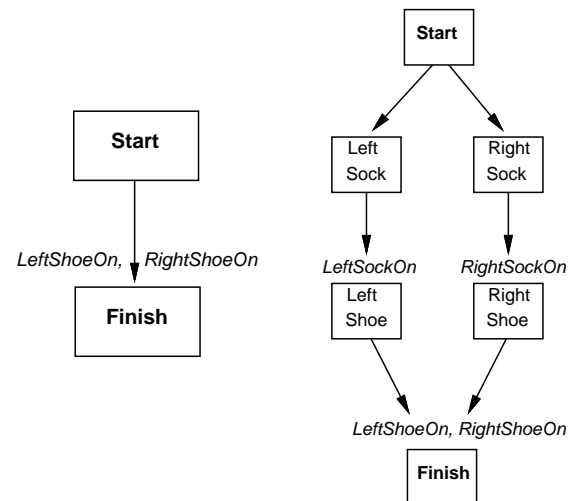
Definition of  $PlanResult$  in terms of  $Result$ :

$$\forall s \text{ PlanResult}([], s) = s$$

$$\forall a, p, s \text{ PlanResult}([a]p, s) = \text{PlanResult}(p, \text{Result}(a, s))$$

Planning systems are special-purpose reasoners designed to do this type of inference more efficiently than a general-purpose reasoner

## Partial Order Planning



## Partial Order Planning

- ◇ sequential planning: forward (or backward) step-by-step search
- ◇ Consider planning a trip to New York by flying
  1. start with finding how to get from home to the Melbourne airport
  2. start with finding how to get from the New York airport to hotel
  3. start with finding a plane ticket from Melbourne to New York
- ◇ least commitment strategy—delay making commitments to steps that are less important/constrained

## Components of Partial Order Planning

- **Actions**
  - “Start” action: no preconditions, effects = initial state
  - “Finish” action: preconditions = goal state, no effects
  - (regular) actions with preconditions and effects
- **Ordering constraints** between actions
  - $A \prec B$ :  $A$  is before  $B$  (partial order)
  - $LeftSock \prec LeftShoe$
- **Causal links** from effect of one action to the precondition of another
  - $A \xrightarrow{c} B$ :  $A$  achieves precondition  $c$  for  $B$
  - $LeftSock \xrightarrow{LeftSockOn} LeftShoe$
  - other actions cannot conflict with the causal link:  $\neg LeftSockOn$
- **Open preconditions**
  - not achieved by any action yet
  - planner: add actions until there are no open preconditions

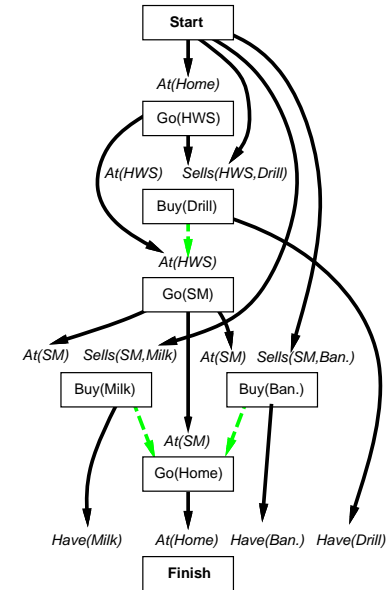
## Example



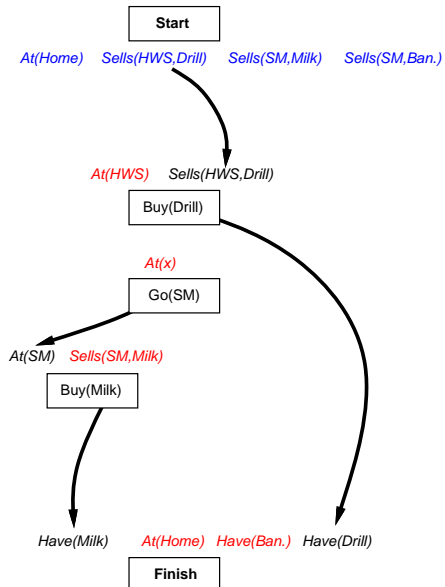
*Have(Milk) At(Home) Have(Ban.) Have(Drill)*

Finish

## Example



## Example



## Planning process

Operators on partial plans:

- add a link from an existing action to an open condition
- add a step to fulfill an open condition
- order one step wrt another to remove possible conflicts

Gradually move from incomplete/vague plans to complete, correct plans

Backtrack if an open condition is unachievable or if a conflict is unresolvable

Topological Sorting in graphs

## POP algorithm sketch

**function** POP(*initial, goal, operators*) **returns** *plan*

*plan* ← MAKE-MINIMAL-PLAN(*initial, goal*)

**loop do**

**if** SOLUTION?(*plan*) **then return** *plan*

$S_{need}, c$  ← SELECT-SUBGOAL(*plan*)

  CHOOSE-OPERATOR(*plan, operators, S<sub>need</sub>, c*)

  RESOLVE-THREATS(*plan*)

**end**

---

**function** SELECT-SUBGOAL(*plan*) **returns**  $S_{need}, c$

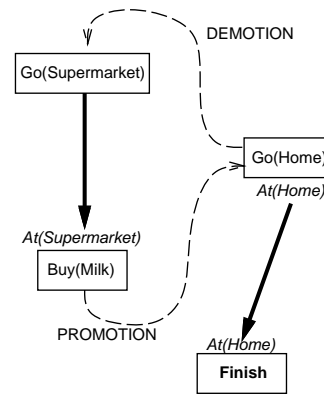
  pick a plan step  $S_{need}$  from STEPS(*plan*)

  with a precondition *c* that has not been achieved

**return**  $S_{need}, c$

## Clobbering and promotion/demotion

A **clobberer** is a potentially intervening step that destroys the condition achieved by a causal link. E.g., *Go(Home)* clobbers *At(Supermarket)*:



Demotion: put before *Go(Supermarket)*

Promotion: put after *Buy(Milk)*

## POP algorithm contd.

**procedure** CHOOSE-OPERATOR(*plan, operators, S<sub>need</sub>, c*)

**choose** a step  $S_{add}$  from *operators* or STEPS(*plan*) that has *c* as an effect

**if** there is no such step **then fail**

  add the causal link  $S_{add} \xrightarrow{c} S_{need}$  to LINKS(*plan*)

  add the ordering constraint  $S_{add} \prec S_{need}$  to ORDERINGS(*plan*)

**if**  $S_{add}$  is a newly added step from *operators* **then**

    add  $S_{add}$  to STEPS(*plan*)

    add  $Start \prec S_{add} \prec Finish$  to ORDERINGS(*plan*)

---

**procedure** RESOLVE-THREATS(*plan*)

**for each**  $S_{threat}$  that threatens a link  $S_i \xrightarrow{c} S_j$  in LINKS(*plan*) **do**

**choose** either

      Demotion: Add  $S_{threat} \prec S_i$  to ORDERINGS(*plan*)

      Promotion: Add  $S_j \prec S_{threat}$  to ORDERINGS(*plan*)

**if not** CONSISTENT(*plan*) **then fail**

**end**

## Properties of POP

Nondeterministic algorithm: backtracks at **choice** points on failure:

- choice of  $S_{add}$  to achieve  $S_{need}$
- choice of demotion or promotion for clobberer
- selection of  $S_{need}$  is irrevocable

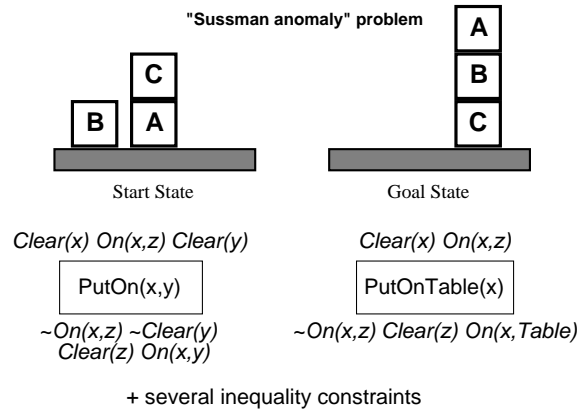
POP is sound, complete, and **systematic** (no repetition)

Extensions for disjunction, universals, negation, conditionals

Can be made efficient with good heuristics derived from problem description

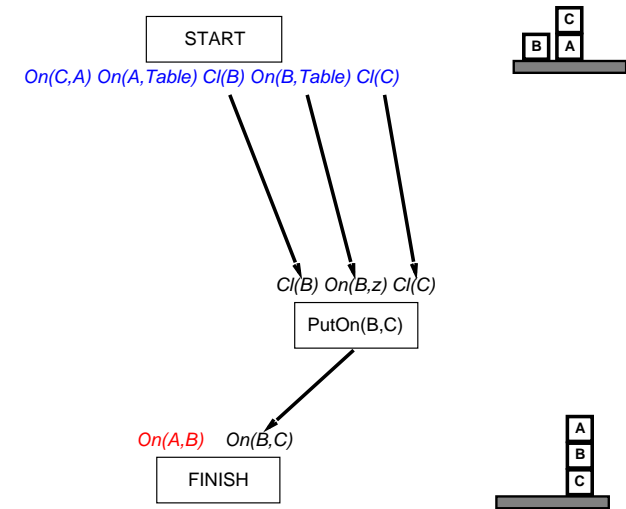
Particularly good for problems with many loosely related subgoals

## Example: Blocks world

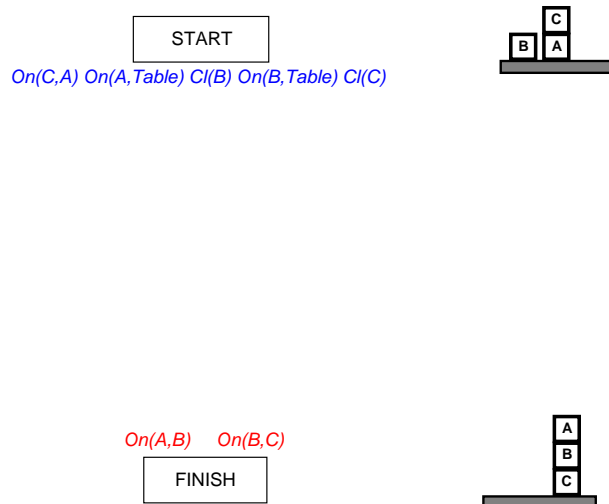


[Linear planners (find a plan for each subgoal and concatenate the plans) can't find a solution]

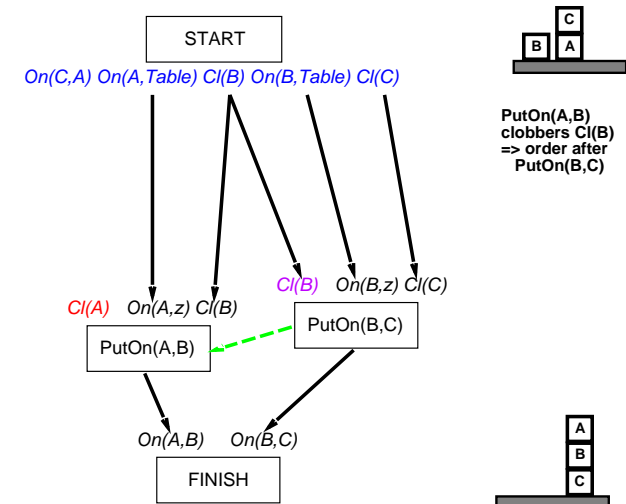
## Example contd.



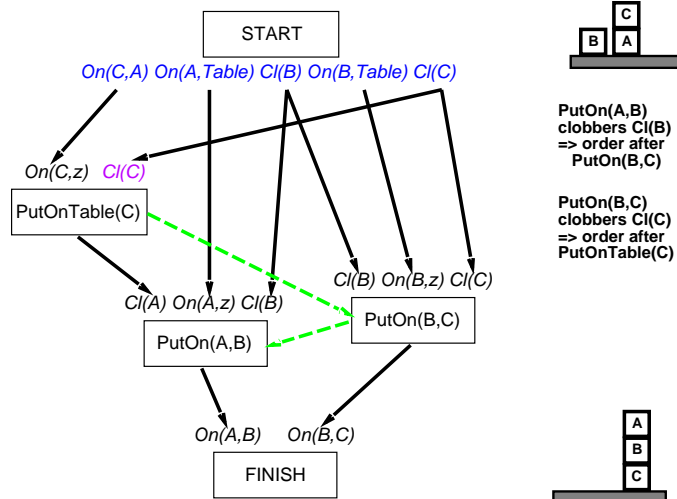
## Example contd.



## Example contd.



## Example contd.



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## Heuristics

◇ Which open precondition to choose?

- most constrained open precondition
  - can be satisfied in the fewest number of ways
- can provide substantial speedups
  - if it can't be satisfied, stop early and return fail
  - if it can be satisfied by only one way, no choice anyhow and can reduce the number of possibilities later on

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