

## Slides for Chapter 11: Time and Global State



From **Coulouris, Dollimore and Kindberg**  
**Distributed Systems:  
Concepts and Design**  
Edition 4, © Pearson Education 2005

Fourth Edition  
**DISTRIBUTED SYSTEMS**  
**CONCEPTS AND DESIGN**  
George Coulouris  
Jean Dollimore  
Tim Kindberg

## Logical time and clocks (11.4)

- ⌘ can't synchronize physical clocks perfectly
- ⌘ absolute time might not be necessary, just need ordering of events
- ⌘ logical clocks: Lamport, 1978
- ⌘ happened-before relationship among events
- ⌘ potential causal ordering

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## Happen-before relation

⌘  $e \rightarrow e'$

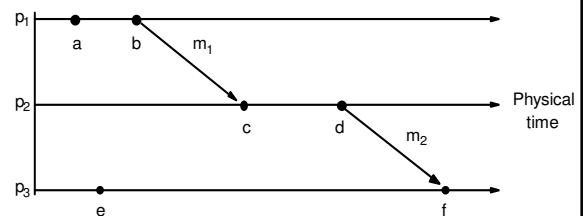
- ☒ two events occur in the same process
- ☒ a message is sent between two processes

⌘ Happened-before relation:

- ☒ HB1: if  $e \rightarrow e'$  in process  $i$ , then  $e \rightarrow e'$
- ☒ HB2: for any message  $m$ ,  $\text{send}(m) \rightarrow \text{receive}(m)$
- ☒ HB3: if  $e \rightarrow e'$  and  $e' \rightarrow e''$ , then  $e \rightarrow e''$

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## Events occurring at three processes



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## Happen-before vs. causality

- ⌘  $e \parallel e'$  if the two events aren't in a particular order (concurrent)
- ⌘ potential causality:  $e \rightarrow e'$  doesn't mean that  $e$  causes  $e'$
- ⌘ naturally, if  $e$  causes  $e'$ ,  $e \rightarrow e'$

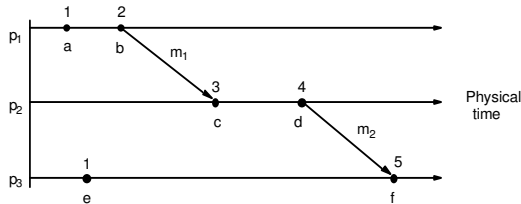
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## Logical clocks (Lamport)

- ⌘ each process  $i$  keeps a local clock  $L_i$
- ⌘ updating logical clocks:
  - ☒ LC1:  $L_i := L_i + 1$  for each event in process  $i$
  - ☒ LC2:
    - ☒ When a process  $i$  sends a message  $m$ 
      - it piggybacks on  $m$  the value of  $t = L_i$
    - ☒ Upon receiving  $(m, t)$ , process  $j$ 
      - computes  $L_j := \max(L_j, t)$  and then
      - applies LC1 before timestamping the event  $\text{receive}(m)$
- ⌘ if  $e \rightarrow e'$ , then  $L(e) < L(e')$
- ⌘ but  $L(e) < L(e')$  doesn't imply  $e \rightarrow e'$ . Why? (Fig. 11.6)

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## Lamport timestamps (Fig 11.6)



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## Totally ordered logical clocks

⌘ different processes, same Lamport time

⌘ Time:  $(T_p, i)$

⌘  $(T_p, i) < (T_j, j)$  iff

☑  $T_i < T_j$ , or

☑  $T_i = T_j$  and  $i < j$

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## Vector clocks

⌘ Lamport clocks:  $L(e) < L(e')$  doesn't imply  $e \rightarrow e'$

⌘ each process keeps its own vector clock  $V_i$

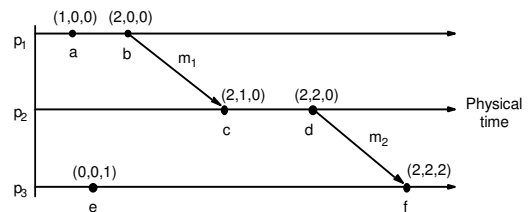
⌘ piggyback timestamps on messages

⌘ updating vector clocks:

- ☑ VC1: Initially,  $V_i[j] := 0$  for  $p_i, j=1..N$  ( $N$  processes)
- ☑ VC2: before  $p_i$  timestamps an event,  $V_i[i] := V_i[i]+1$
- ☑ VC3:  $p_i$  piggybacks  $t = V_i$  on every message it sends
- ☑ VC4: when  $p_j$  receives a timestamp  $t$ , it sets  $V_j[k] := \max(V_j[k], t[k])$  for  $k=1..N$  (merge operation)

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## Vector timestamps (Fig 11.7)



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## Vector clocks

⌘ At  $p_i$

- ☑  $V_i[i]$  is the number of events  $p_i$  timestamped locally
- ☑  $V_i[j]$  is the number of events that have occurred at  $p_j$  (that has potentially affected  $p_i$ )
- ☑ Could more events than  $V_i[j]$  have occurred at  $p_j$ ?

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## Comparing vector timestamps

⌘  $V = V'$  iff

☑  $V[j] = V'[j], j = 1..N$

⌘  $V \leq V'$  iff

☑  $V[j] \leq V'[j], j = 1..N$

⌘  $V < V'$  iff

☑  $V < V'$  and  $V \neq V'$

☑ Different from  $<$  in all elements

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## Vector timestamps

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⌘ if  $e \rightarrow e'$ , then  $V(e) < V(e')$

⌘ if  $V(e) < V(e')$ , then  $e \rightarrow e'$ . (Exercise 11.13)

☒ Figure 11.7

☒ neither  $V(c) \leq V(e)$  nor  $V(c) \geq V(e)$

☒  $c \parallel e$

⌘ Disadvantage compared to Lamport timestamps?